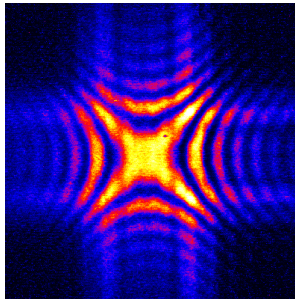
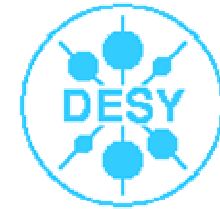


**RWTH**



# A Double Slit Experiment to Study the Transverse Coherence of the TTF Free Electron Laser

Rasmus Ischebeck

# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

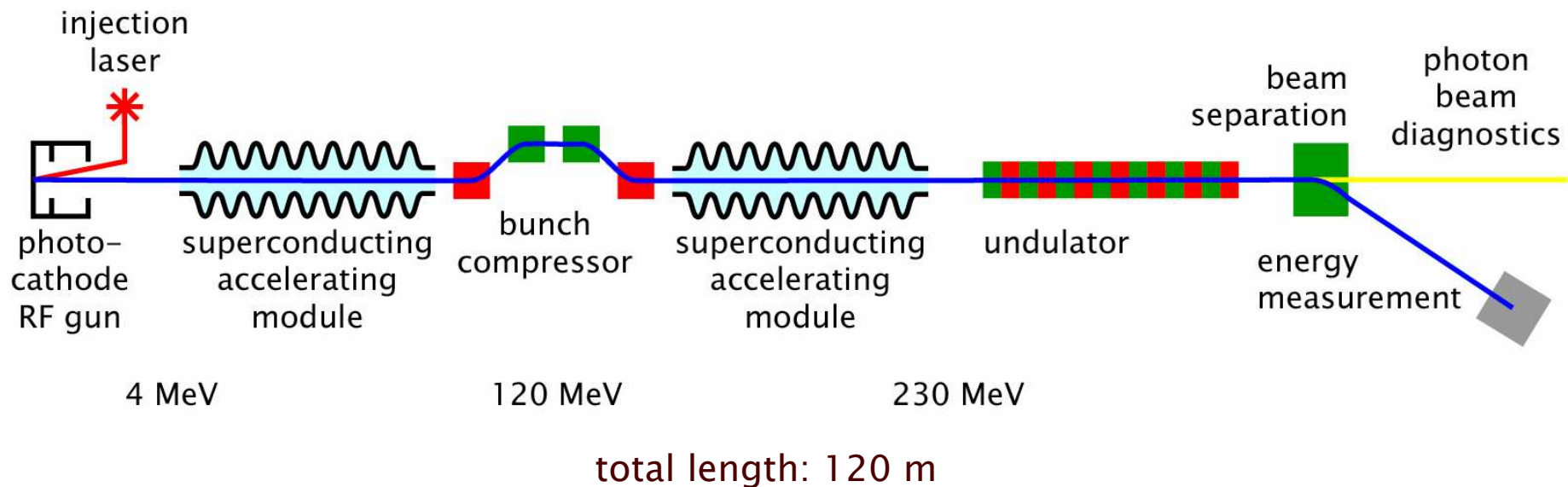
- Introduction
  - TTF Linear Accelerator and Free Electron Laser
  - Photon Diagnostics
  - Near Field Diffraction Effects
- Measurements
- Image Processing
- Analysis
- Simulations
- Consistency of the Measurements
- Development of Transverse Coherence
- Outlook

# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

- Introduction
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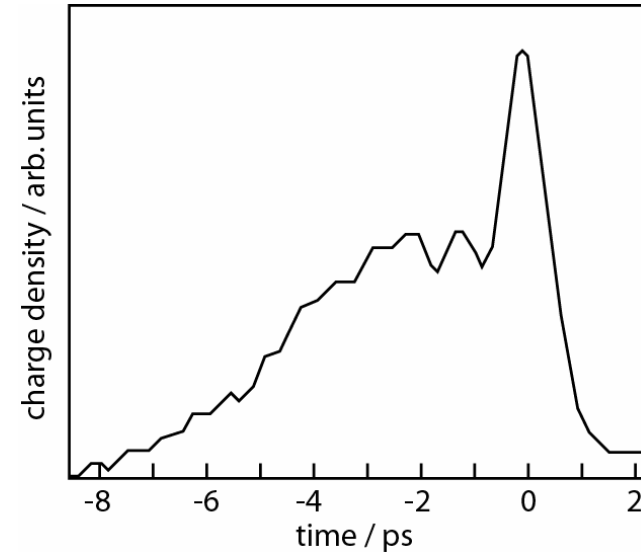
# TTF FEL Linear Accelerator

- Gun
- Superconducting RF Cavities
- Bunch Compressor
- Undulator
- SASE



# Properties of the Electron Bunch

- Energy: 230 MeV per particle
- Bunch charge: 3 nC  
(Radiating bunch charge: 0.2 nC)
- Beam current  $> 1$  kA
- Up to 70 bunches per second

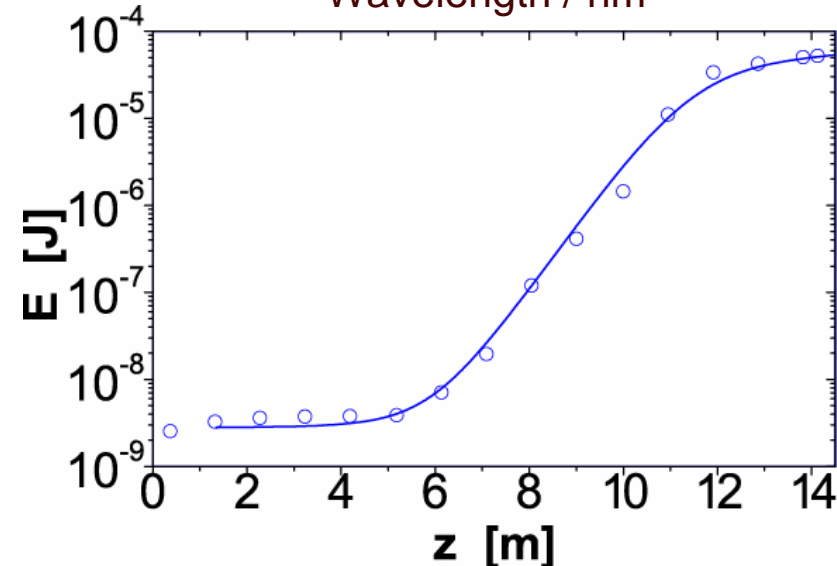
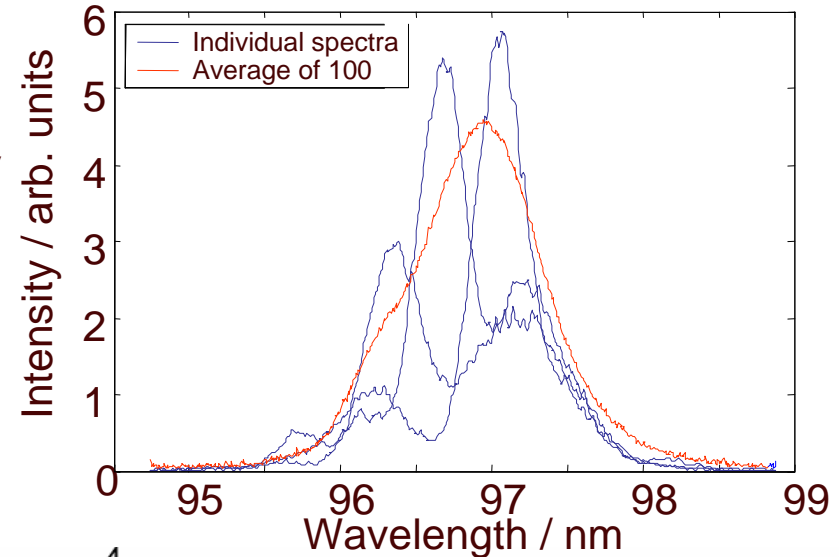


Measurement by  
interferometry of coherent  
transition radiation

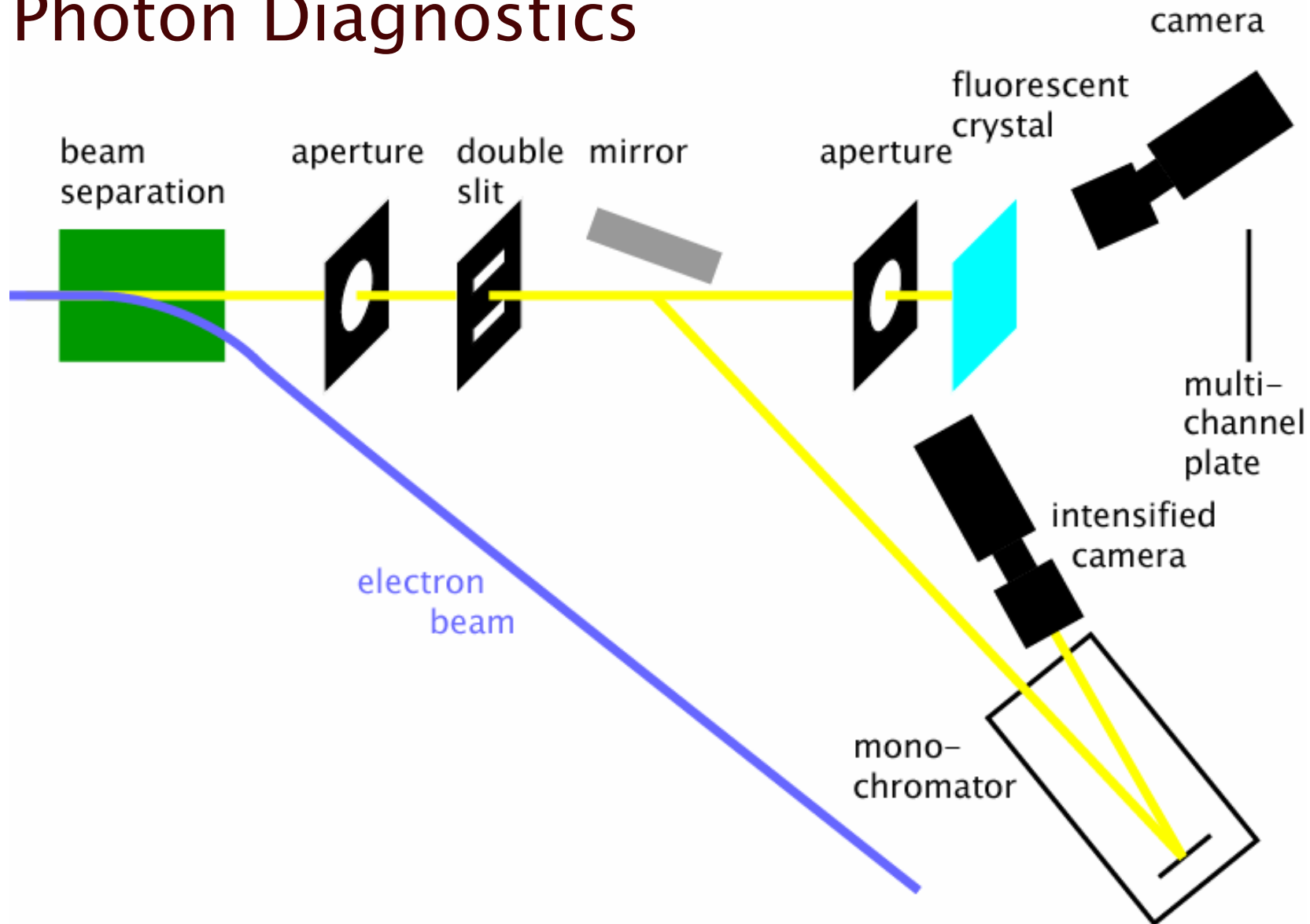
## Experimental Set-Up

# Properties of the FEL Light

- Wavelength: 80 ... 120 nm, depending on the electron energy
- Pulse energy: typically up to 10  $\mu$ J per pulse
- Peak power: 1 GW
- FEL starts from noise
- ⇒ No input needed
- Single pass saturation
- ⇒ No mirrors needed
- Longitudinal and Transverse Coherence

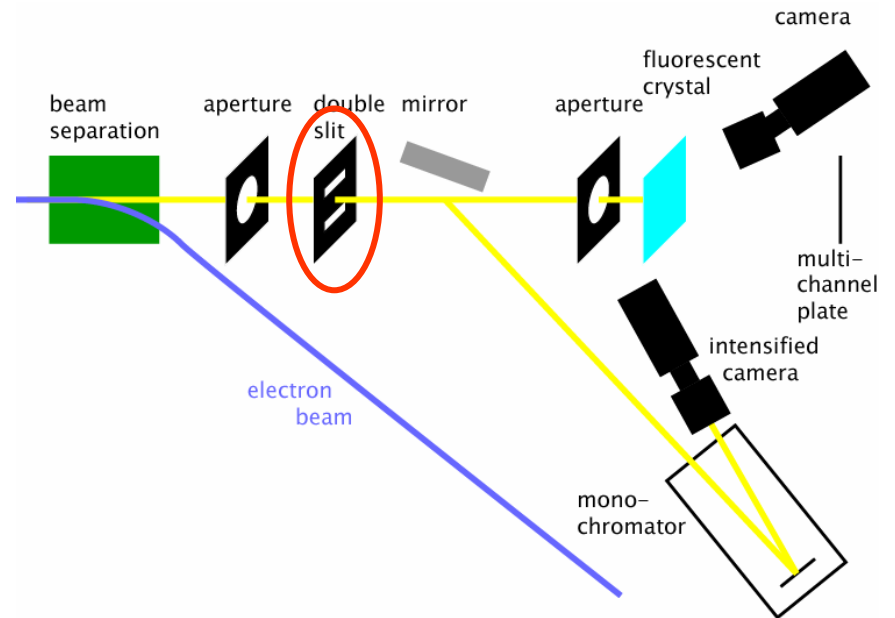
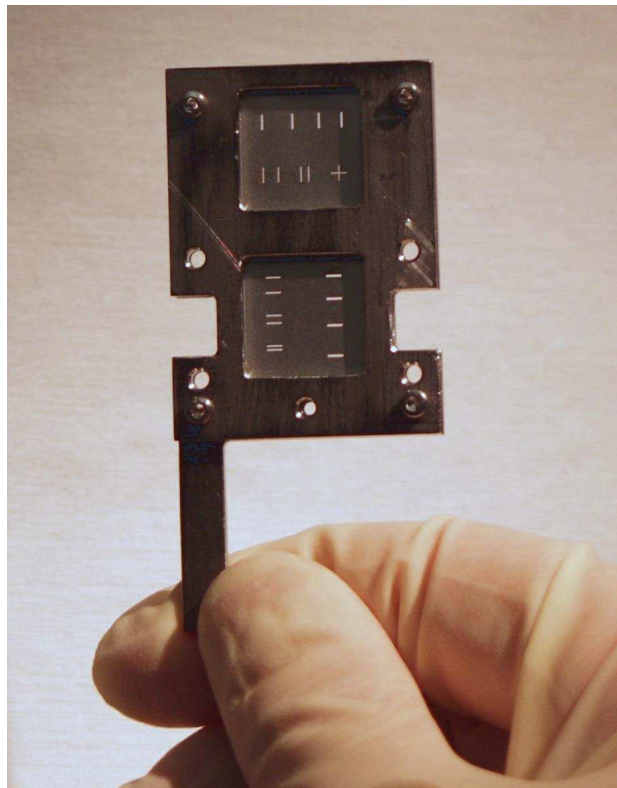


# Experimental Set-Up Photon Diagnostics



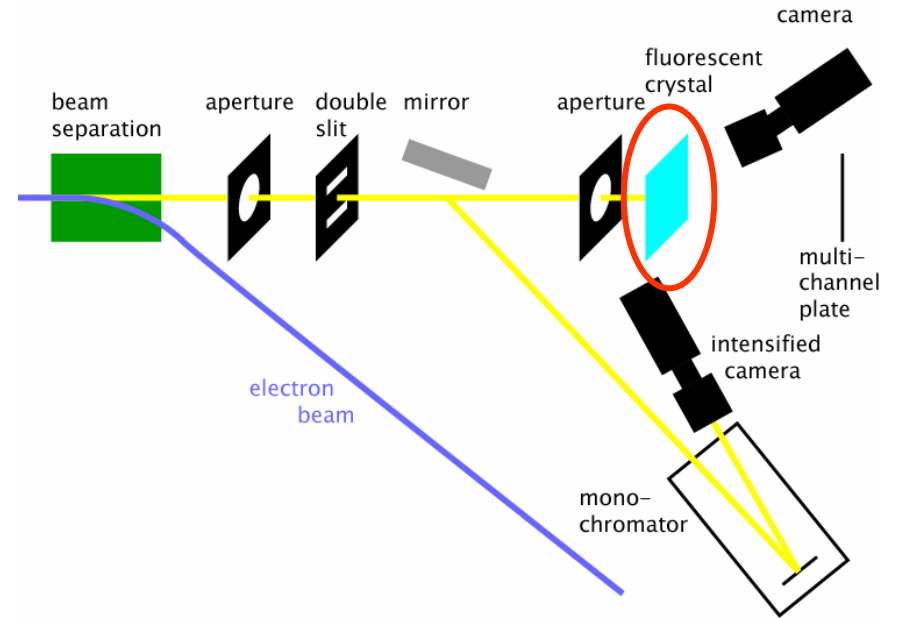
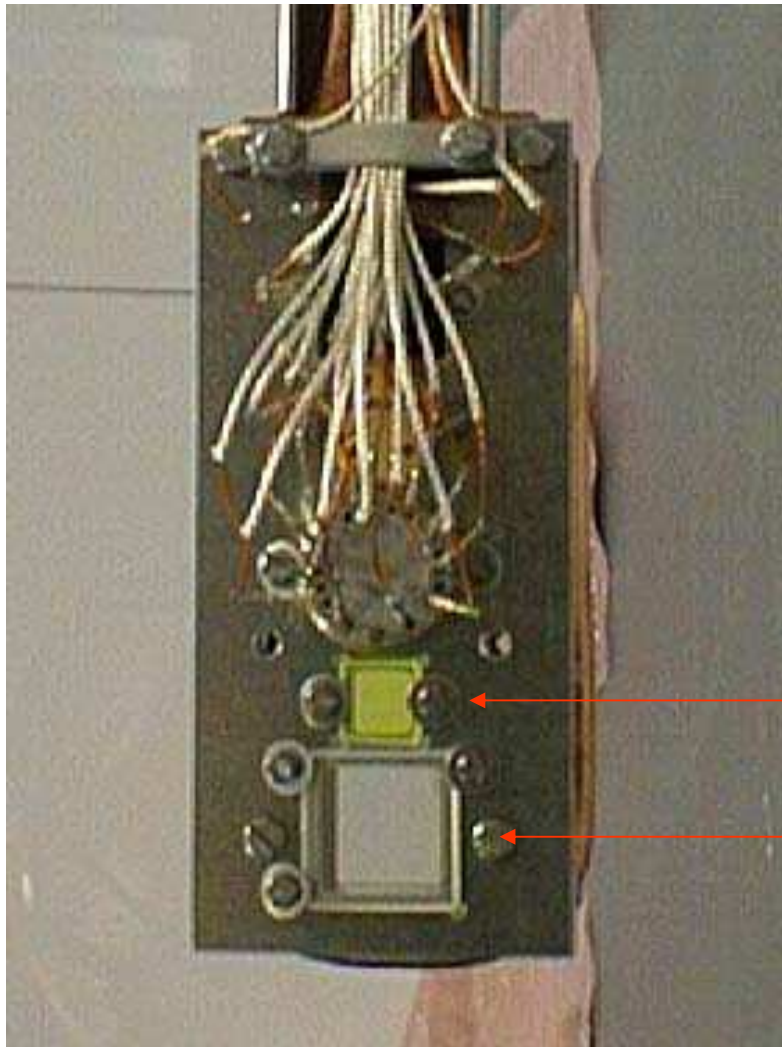
# Experimental Set-Up Double Slits

- Cut in stainless steel foil, using a laser



- Slit separations of 0.5, 1, 2 and 3mm available
- Slit width: 100 $\mu$ m
- Slit length: 2mm
- Can be moved by two stepper motors

# Experimental Set-Up Fluorescent Crystals

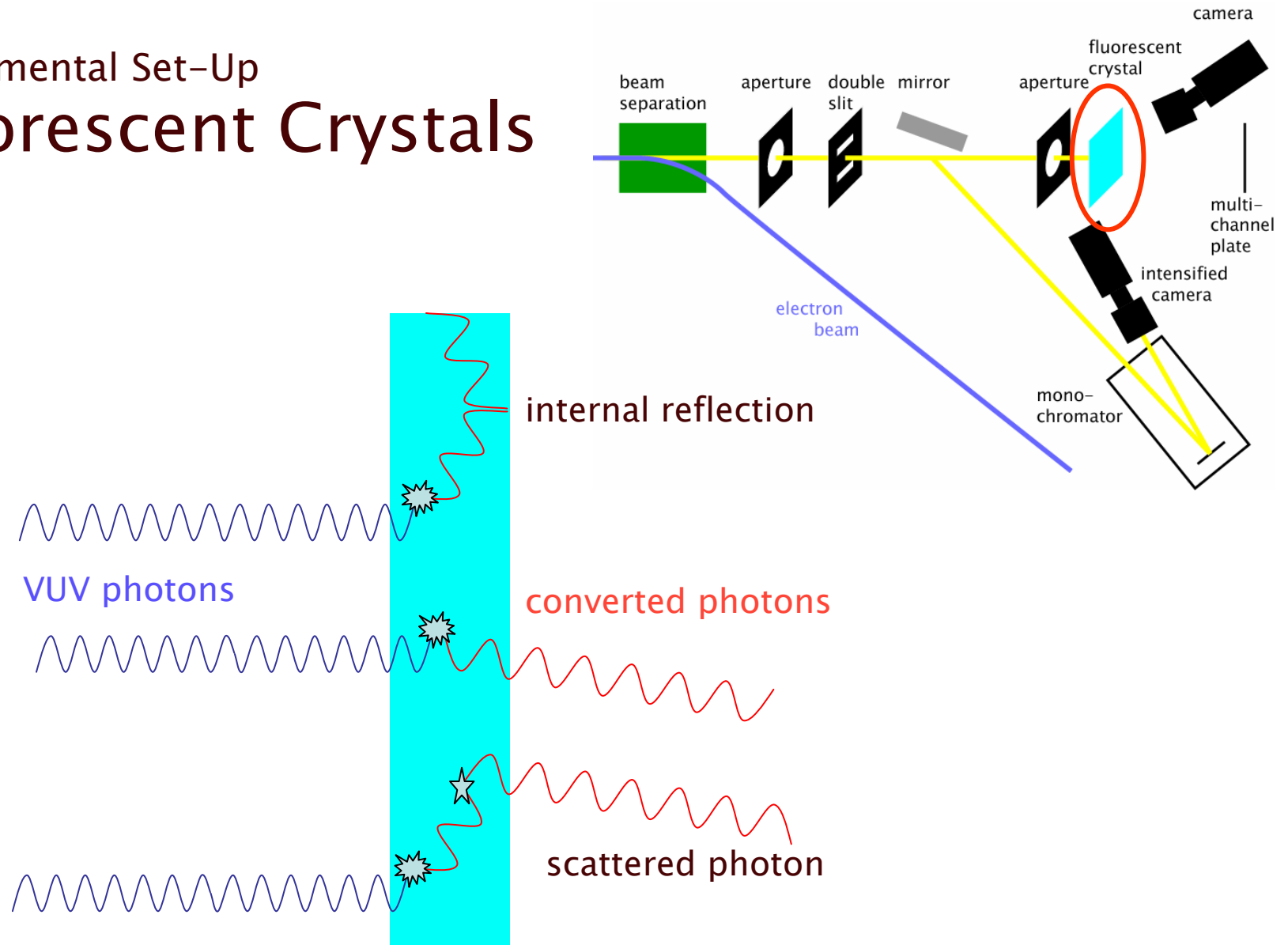


Ce:YAG crystal

PbWO<sub>4</sub> crystal

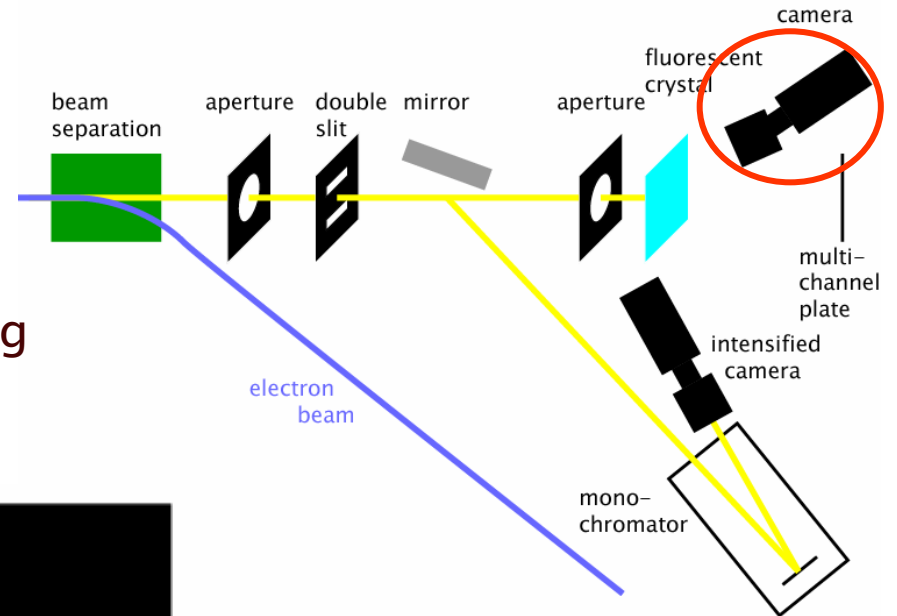
placed on a watercooled frame

# Experimental Set-Up Fluorescent Crystals

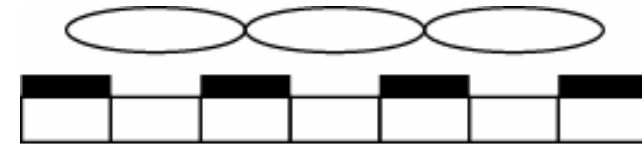


# Experimental Set-Up Camera

- Tilted lens to achieve good focusing over the inclined crystal



- Interline transfer CCD
  - ⇒ fast exposure times
  - ⇒ single-shot measurements
- Lens-on-chip technique
  - ⇒ good sensitivity
- Control and readout over fibre optical link



Experimental Set-Up

# Coherence Measurements

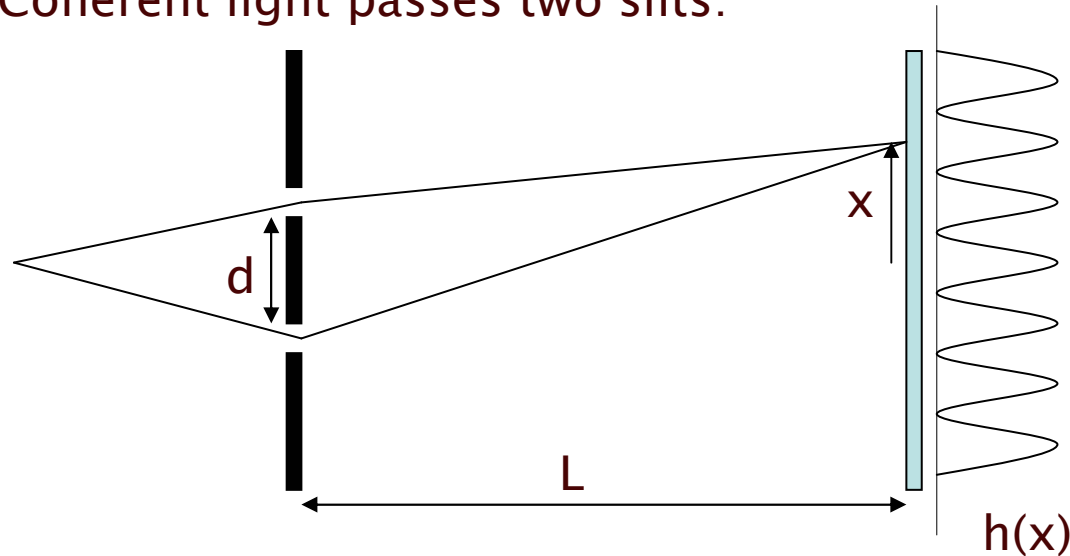
- Diagnostics inside the accelerator tunnel
- Slits, crystal are in the UHV of the linear accelerator
- Distances fixed by set-up
- Near field diffraction
- compared to approx. 3 mm size of the radiation spot:  
slit length 2 mm

# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

- Introduction
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# Young's Double Slit

- Coherent light passes two slits:



In the far field, we have:

$$h(x) = I_0 \left( 1 + \cos\left(2\pi \frac{d}{L\lambda} x\right) \right)$$

Longitudinal (temporal)  
and transverse (spatial)  
coherence necessary!



## Experimental Set-Up

# Near Field Effects

- Criterion for far field diffraction:

$$\frac{\lambda L}{d^2} \gg 1$$

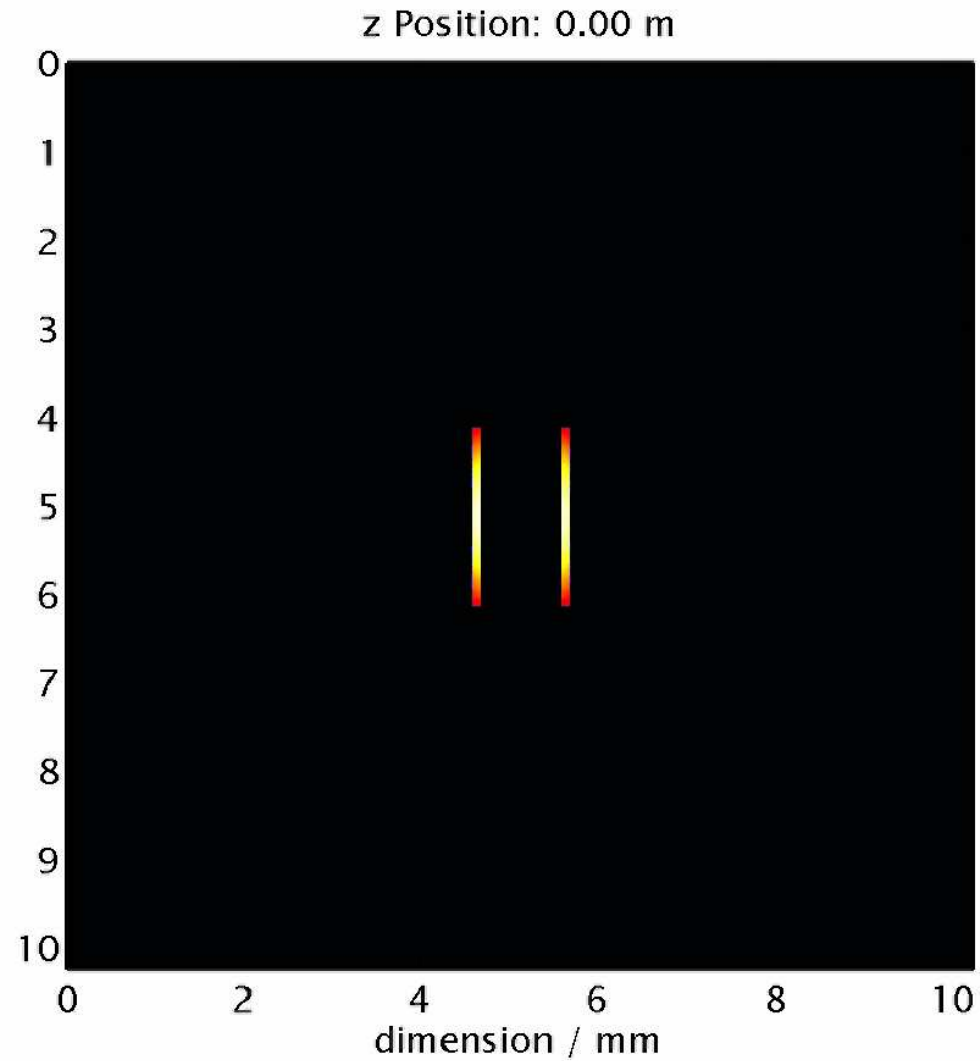
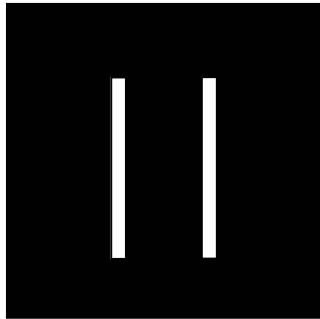
- $d$ : distance between slits,  $\lambda$ : wavelength,  $L$ : distance slits—screen

- Here:  $L = 3.1 \text{ m}$ ,  $d = 1 \text{ mm}$ ,  $\lambda = 100 \text{ nm} \Rightarrow \frac{\lambda L}{d^2} = 0.3$

- Near field effects  $\Rightarrow$  reduced modulation

- additional modifications to the far field formula:
  - finite width and length of slits

# Simulation of Near Field Diffraction

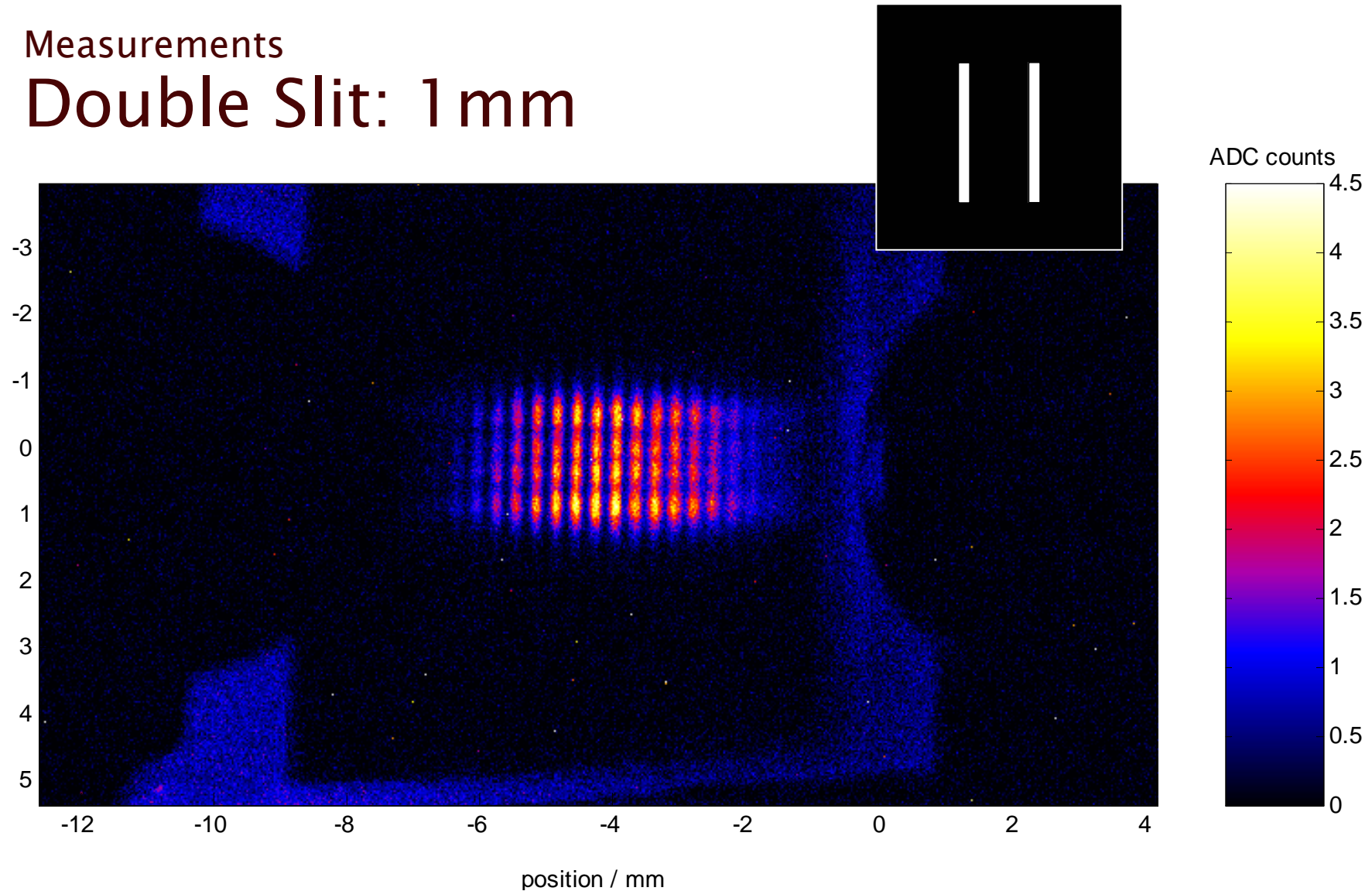


# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

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Measurements

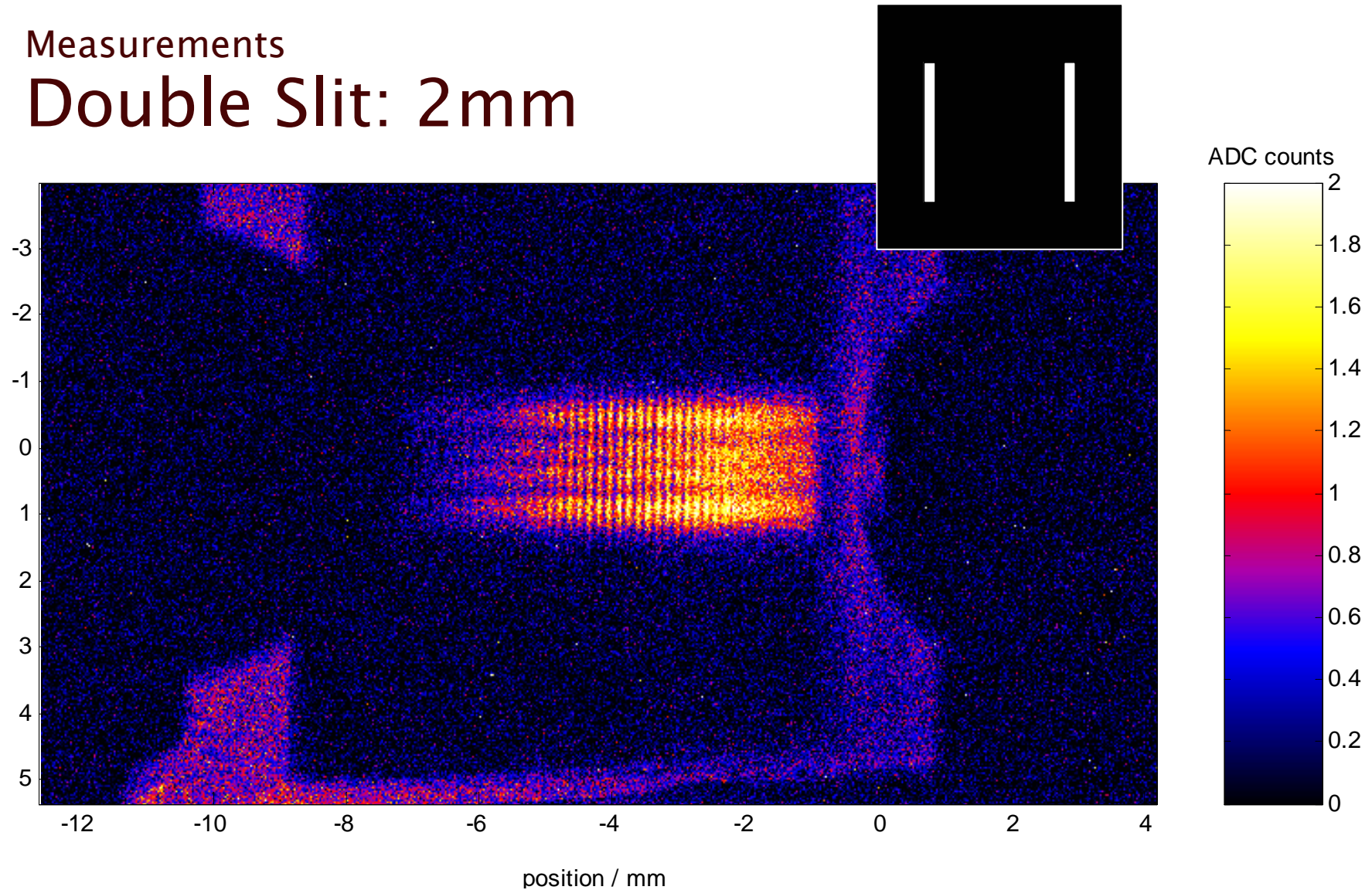
# Double Slit: 1 mm



Vertical slits, 1 mm separation. Average of 99 images with 3 bunches each

Measurements

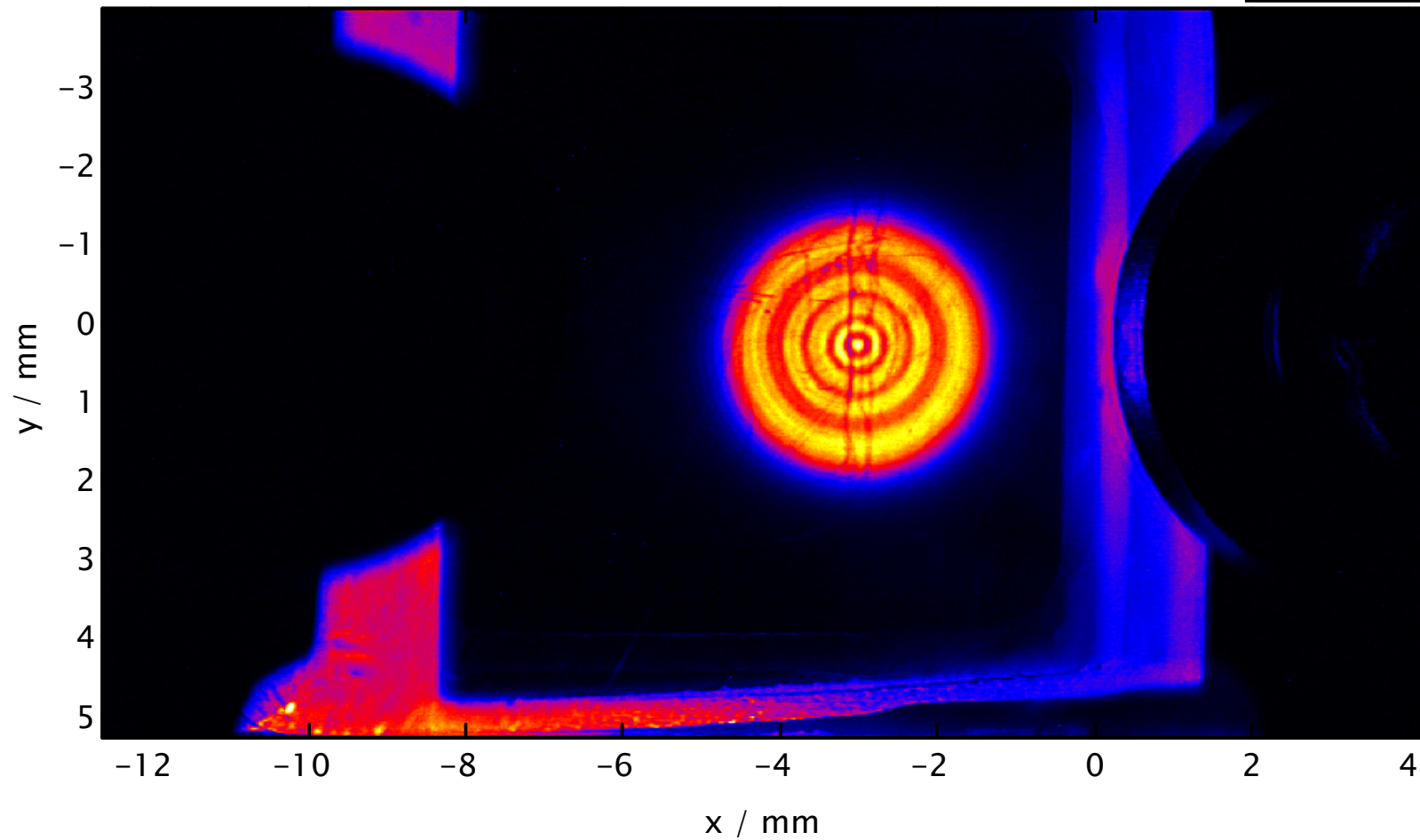
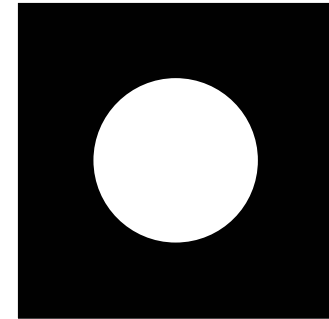
# Double Slit: 2mm



Vertical slits, 2 mm separation. Average of 99 images with 3 bunches each

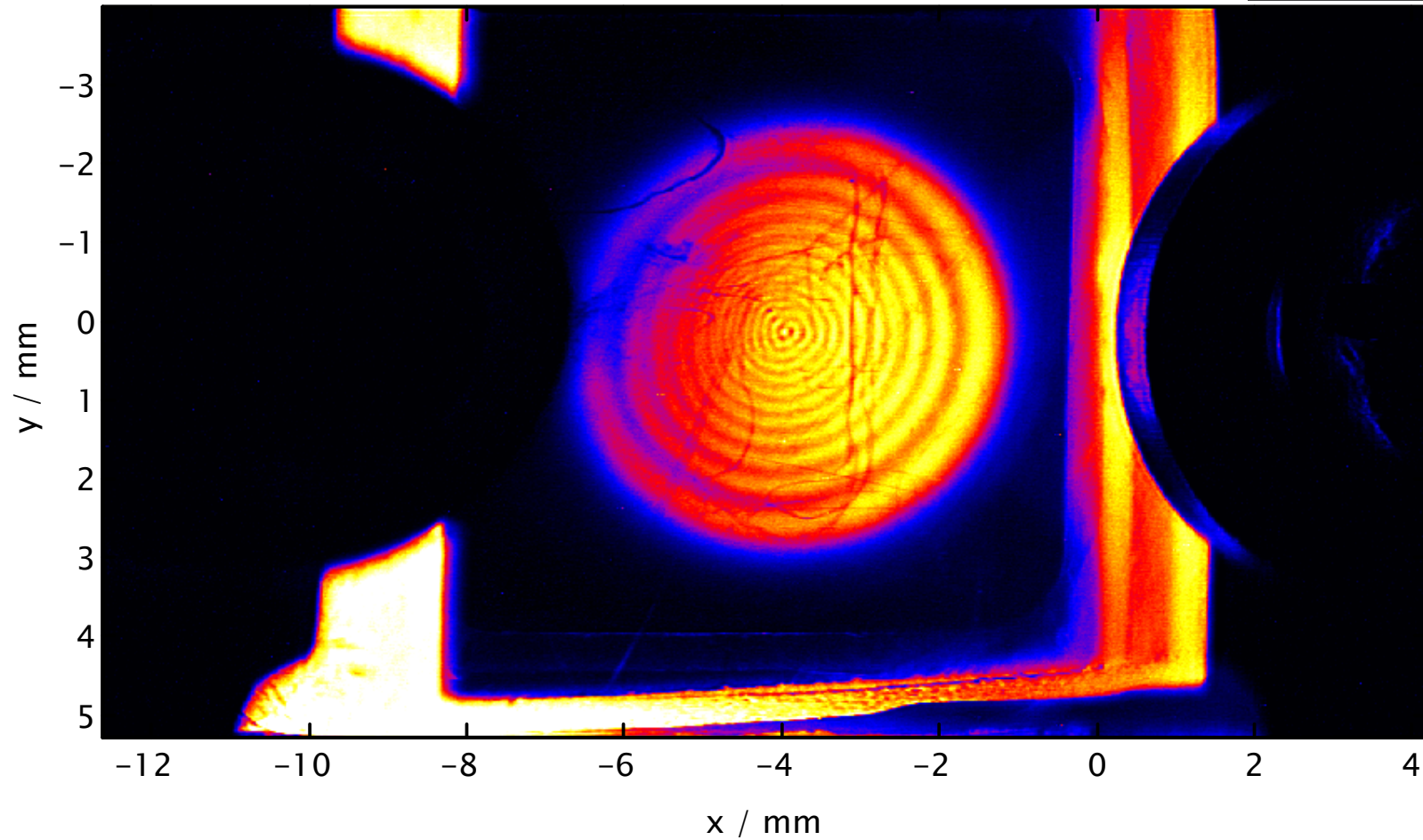
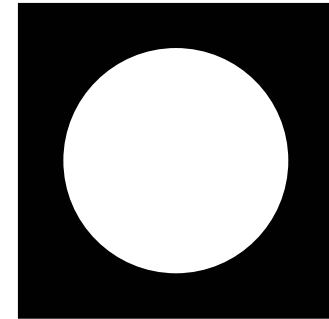
Measurements

# Circular Aperture: $\varnothing$ 3mm



Measurements

# Circular Aperture: $\varnothing$ 5mm



## Measurements

# Circular Apertures

- Number of rings that a circular aperture creates in near field approximation:

$$N_f = \frac{r^2}{\lambda} \left( \frac{1}{D} + \frac{1}{L} \right)$$

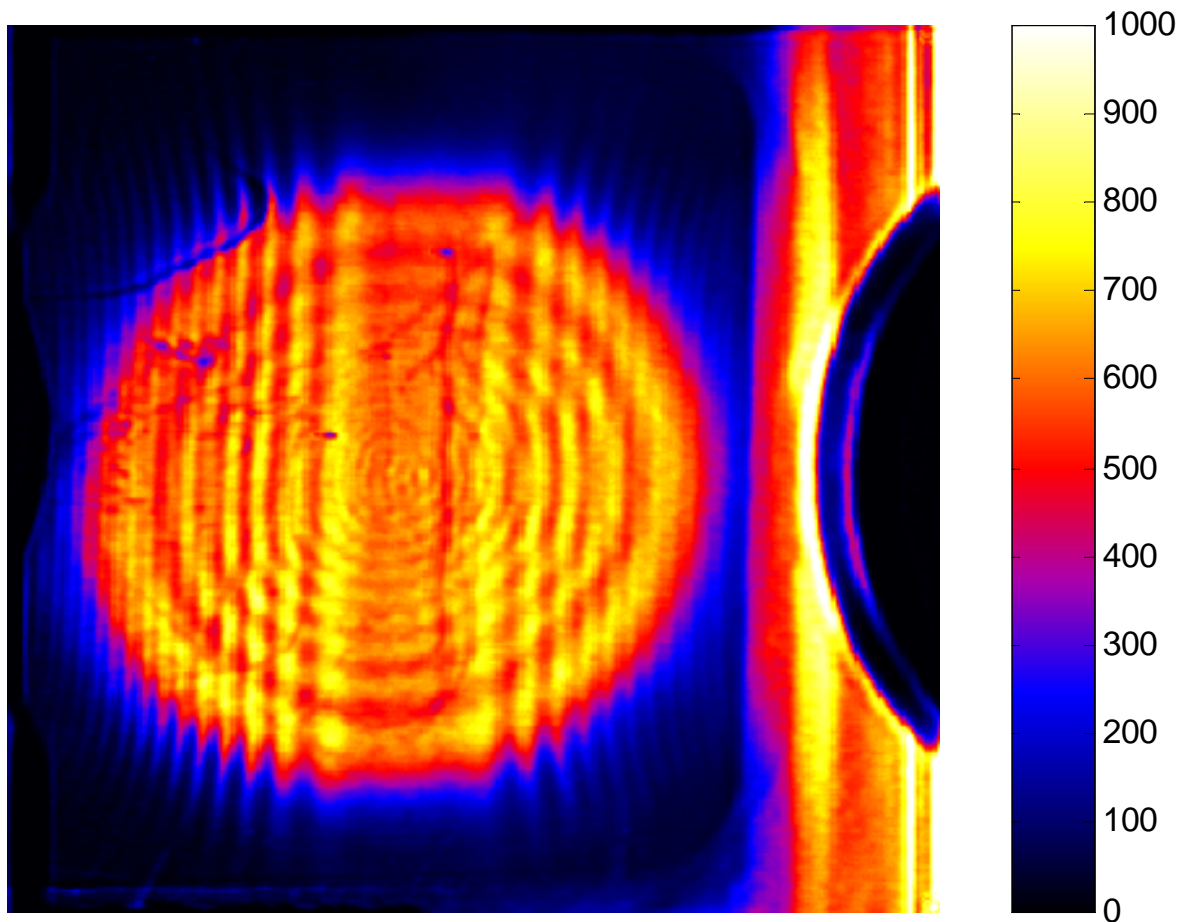
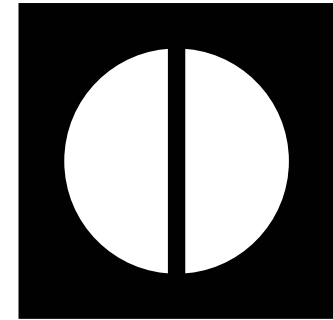
r: aperture radius,  $\lambda$ : wavelength, D: distance source—aperture, L: distance aperture—screen

Here:

Aperture	predicted	observed
3 mm	9.2	9
5 mm	25.5	23

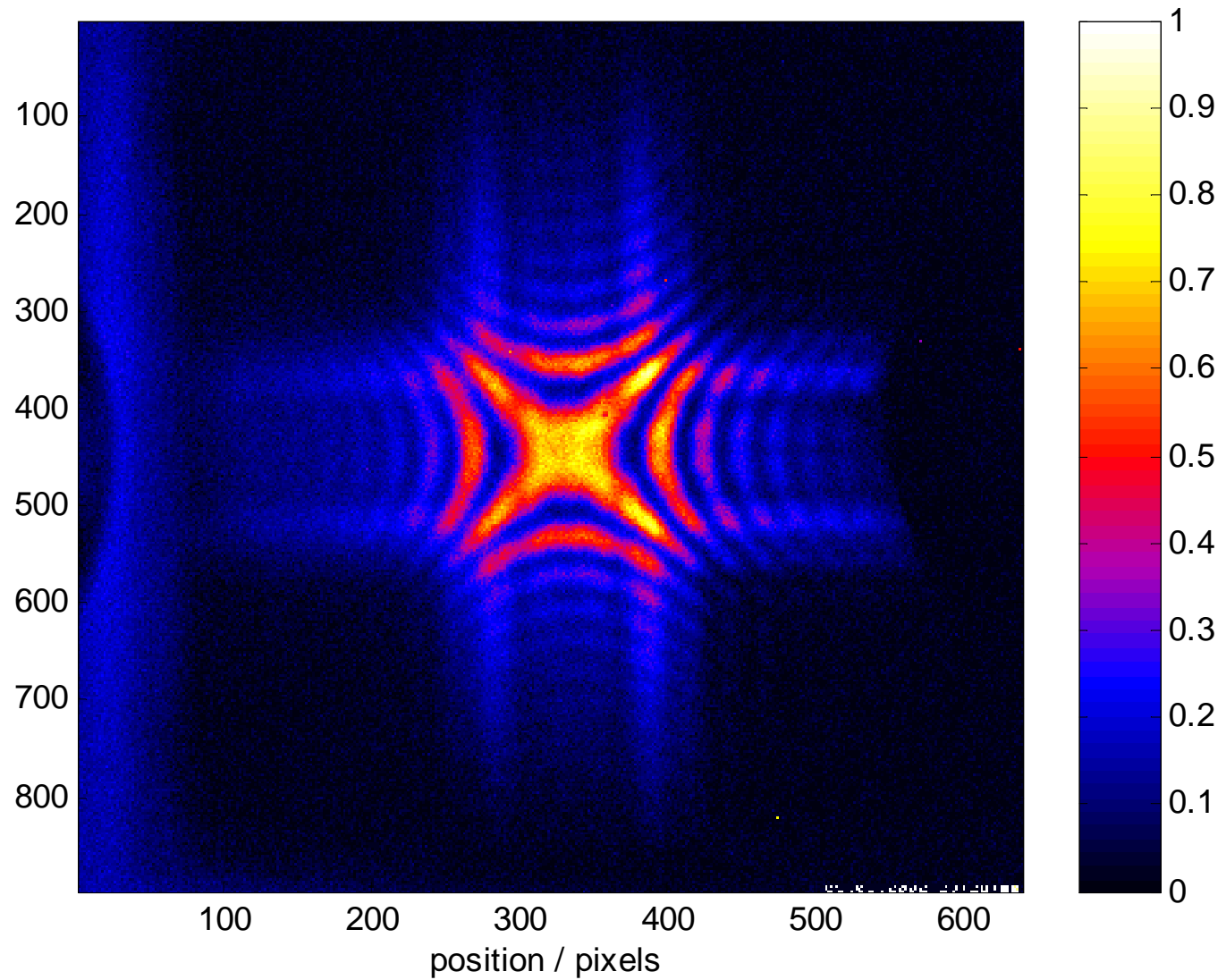
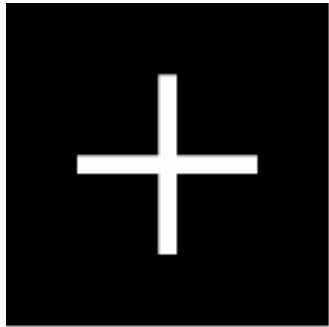
Measurements

# Circular Aperture + Wire



A wire in the beam path also creates diffraction

# Measurements Crossed Slits



# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

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# Deconvolution of the Camera Resolution

- Diffraction effects and lens errors affect the observed image: the real distribution  $\Psi$  is convoluted with the Point Spread Function  $P$

$$\Phi(x, y) = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} P(x - u, y - v) \cdot \Psi(u, v) du dv$$

- For discrete values:

$$\Phi_{i,k} = \sum_{m,n} P_{i-m,k-n} \cdot \Psi_{m,n}$$

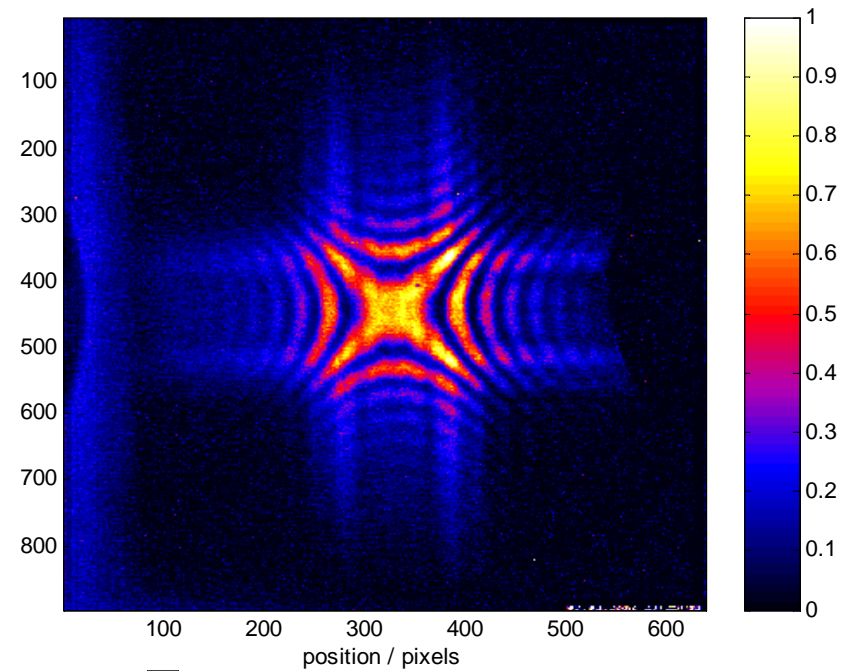
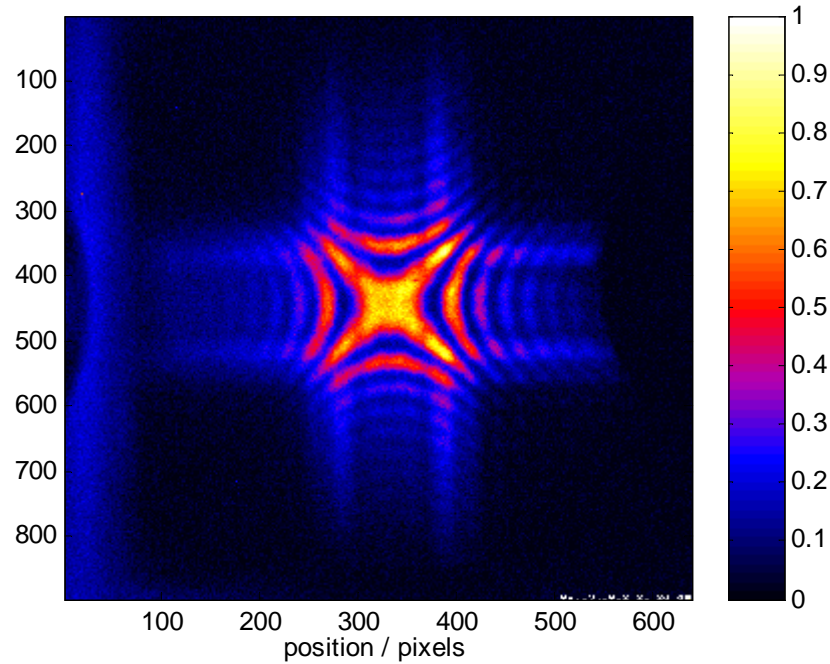
- ⇒ Reduced contrast  
⇒ apparently reduced FEL coherence

# Deconvolution of the Camera Resolution

$$\Phi_{i,k} = \sum_{m,n} P_{i-m,k-n} \cdot \Psi_{m,n}$$

- If P is known, the system of equations can in principle be solved
- But: as a result of measurement errors (noise) in the measured image, negative values for the real intensities will appear!
- The images can be reconstructed using the Lucy–Richardson algorithm
  - Maximize the likelihood of the measurement, with given boundary conditions
  - Widely used in image processing

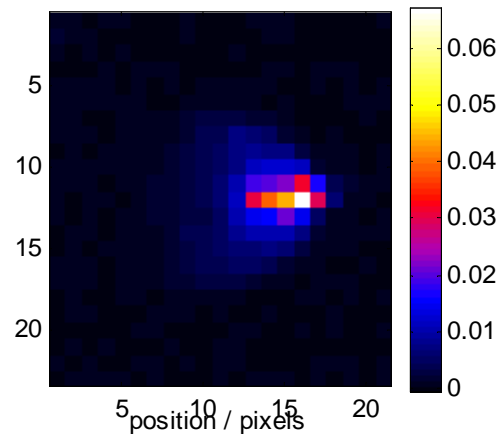
# Deconvolution of the Camera Resolution



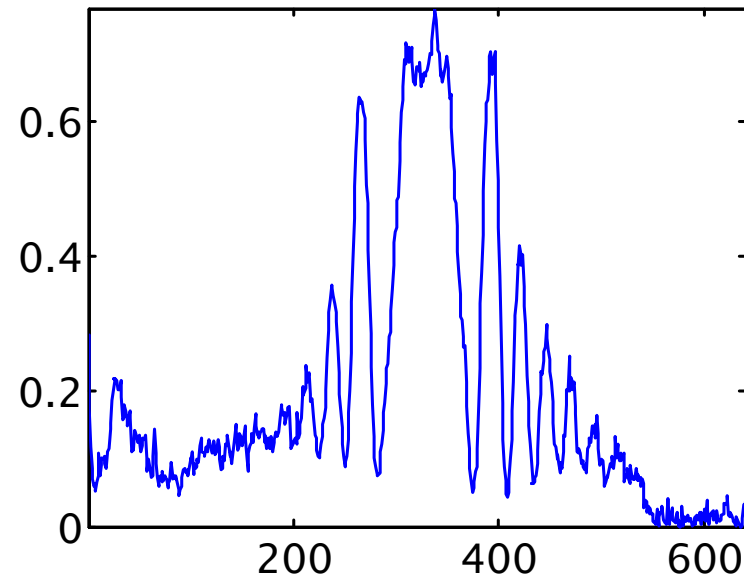
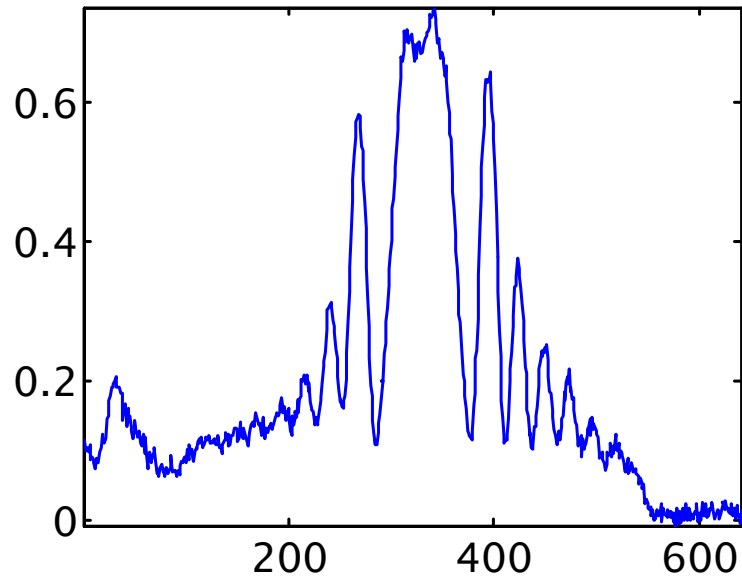
Measured distribution  $\Phi$

Reconstructed distribution  $\Psi$

Point spread function  $P$



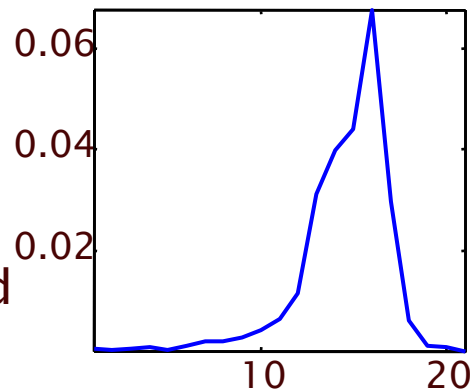
# Deconvolution of the Camera Resolution



Measured distribution  $\Phi$

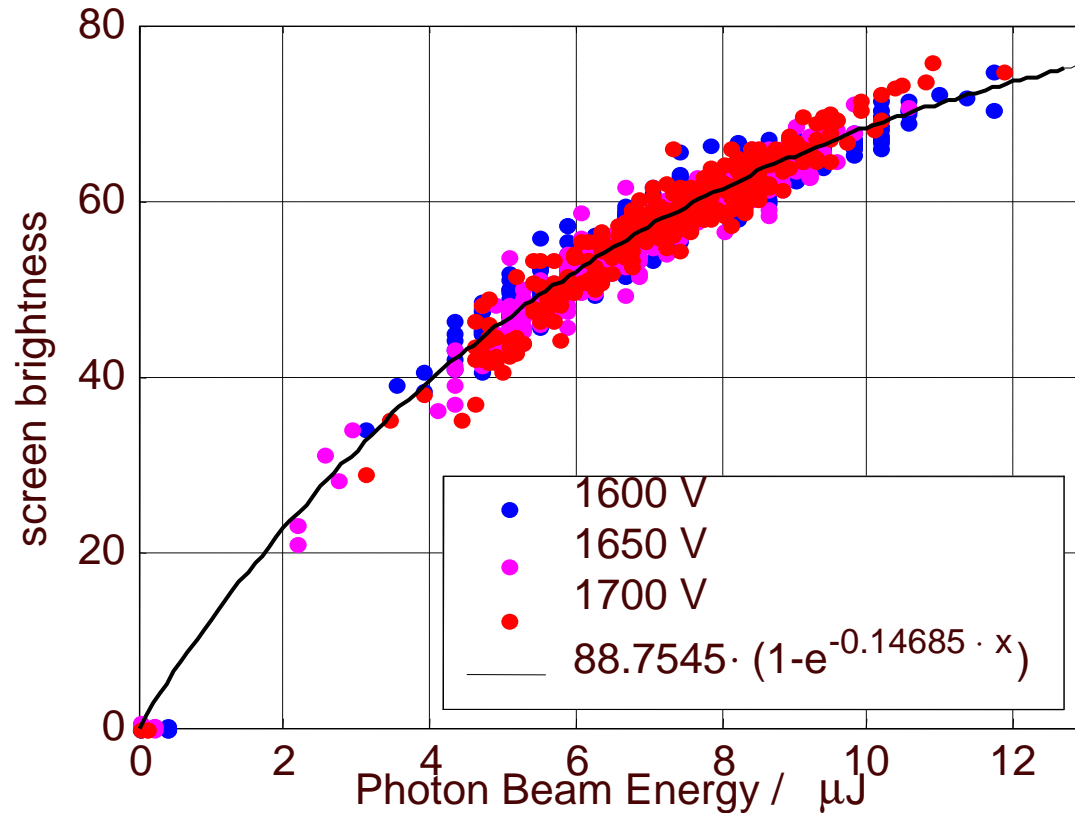
Reconstructed distribution  $\Psi$

Point spread function  $P$



# Correction for Non-Linear Response

- Light emitted by the Ce:YAG crystal is not proportional to the incident energy
- Correction applied with the help of a calibrated multi-channel plate



# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

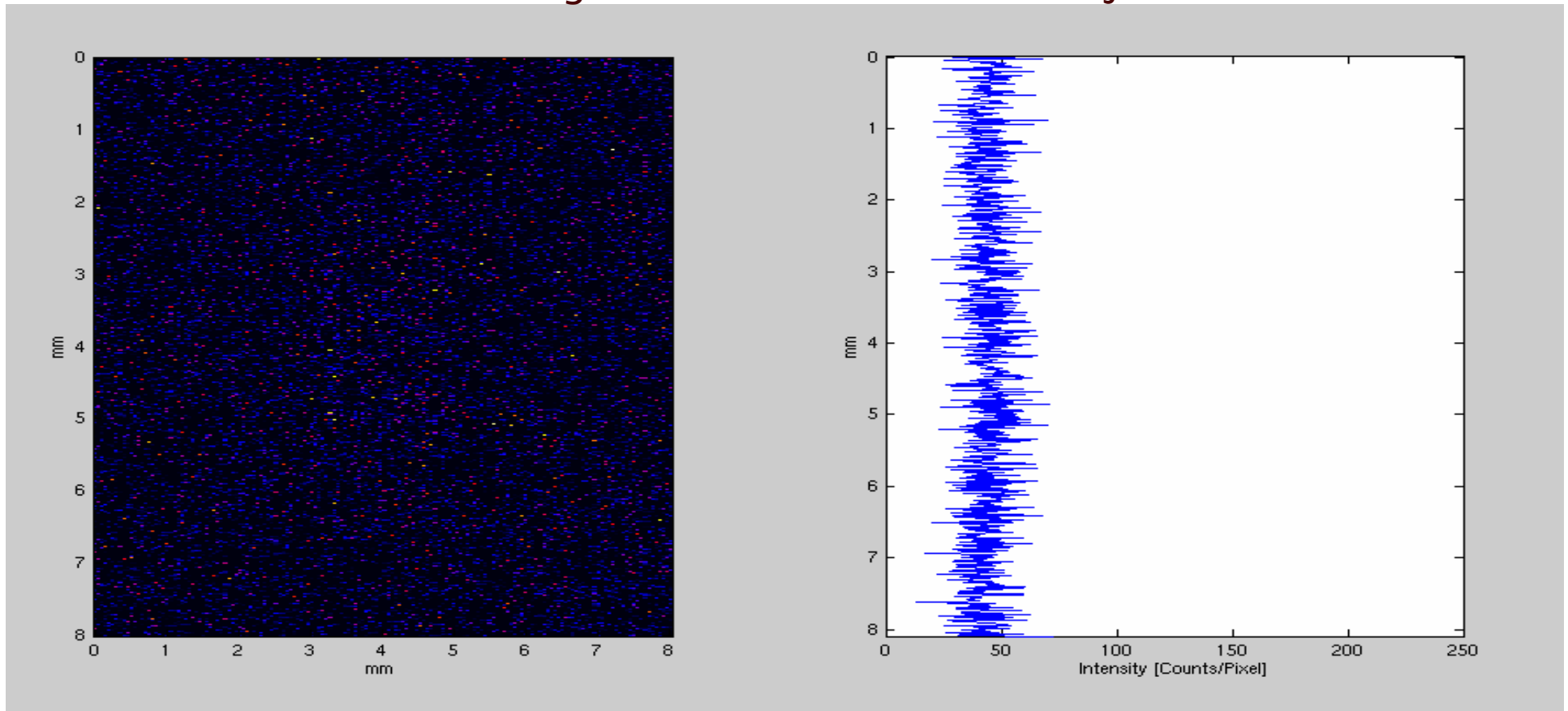
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Experimental Data

# Double Slit — 1 mm separation

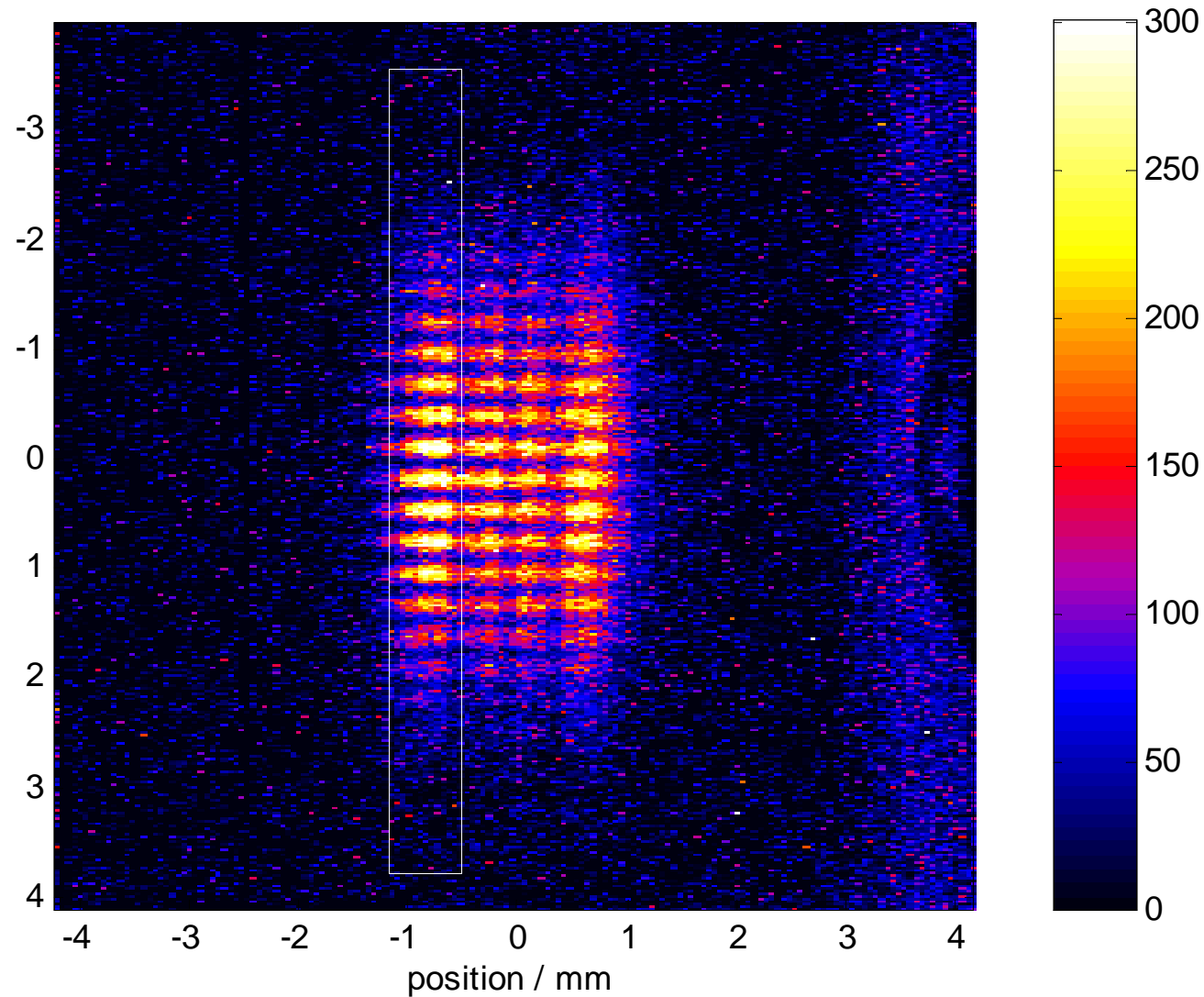
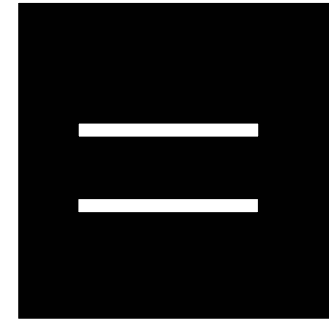
Reconstructed Image

Projection



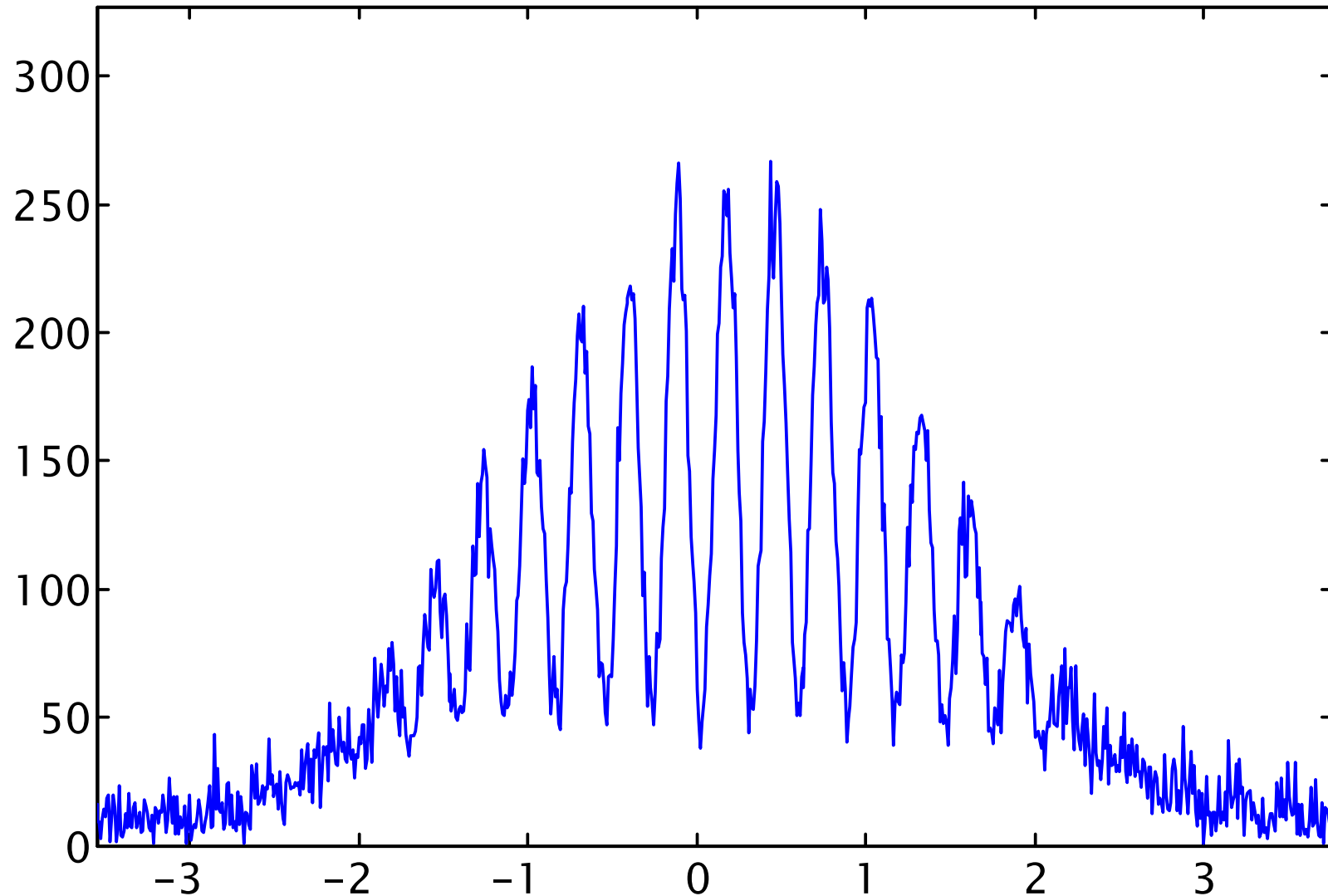
Analysis

# Measurement, 1 mm double slit



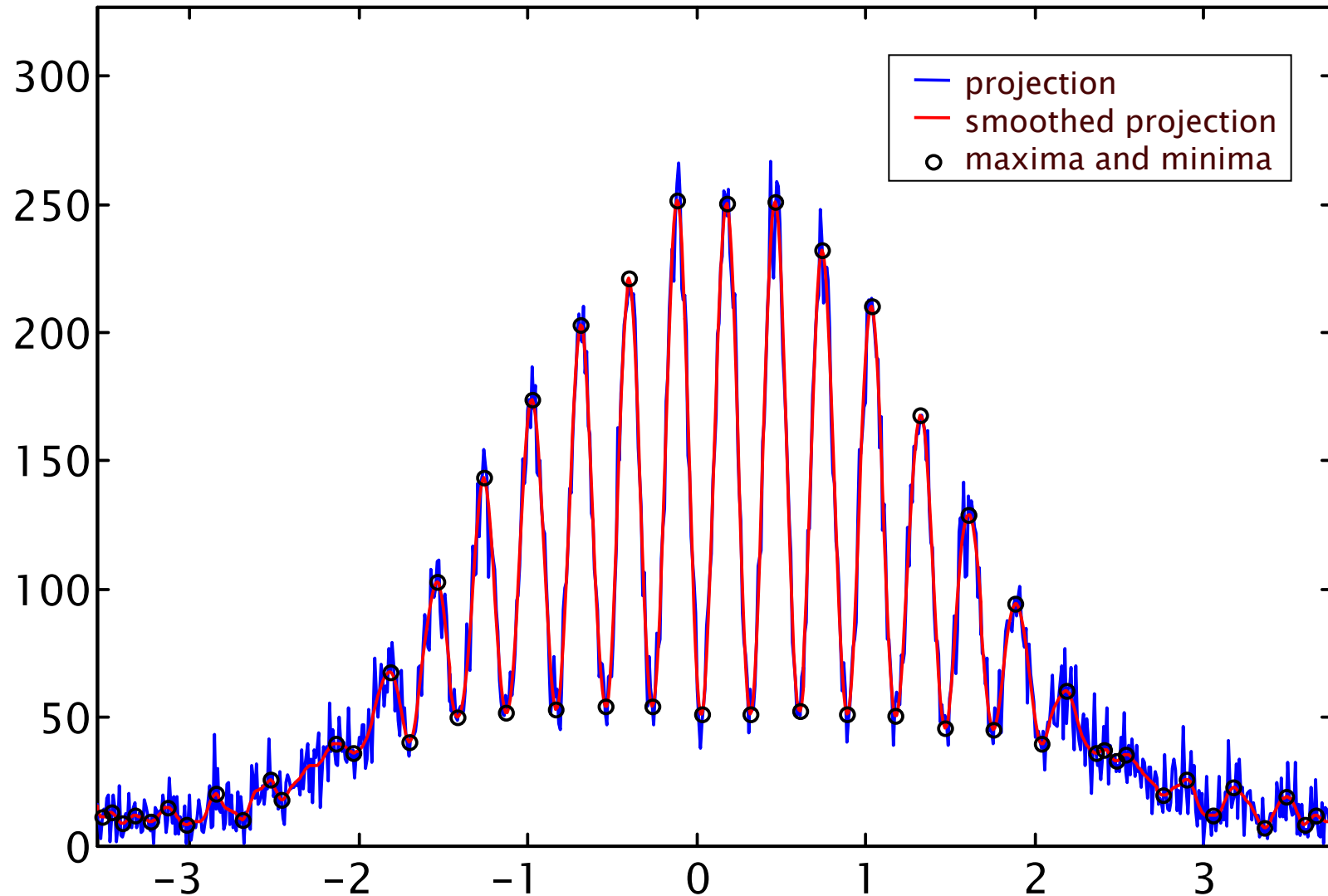
Analysis of Experimental Data

# Projection of the Selected Area



# Analysis of Experimental Data

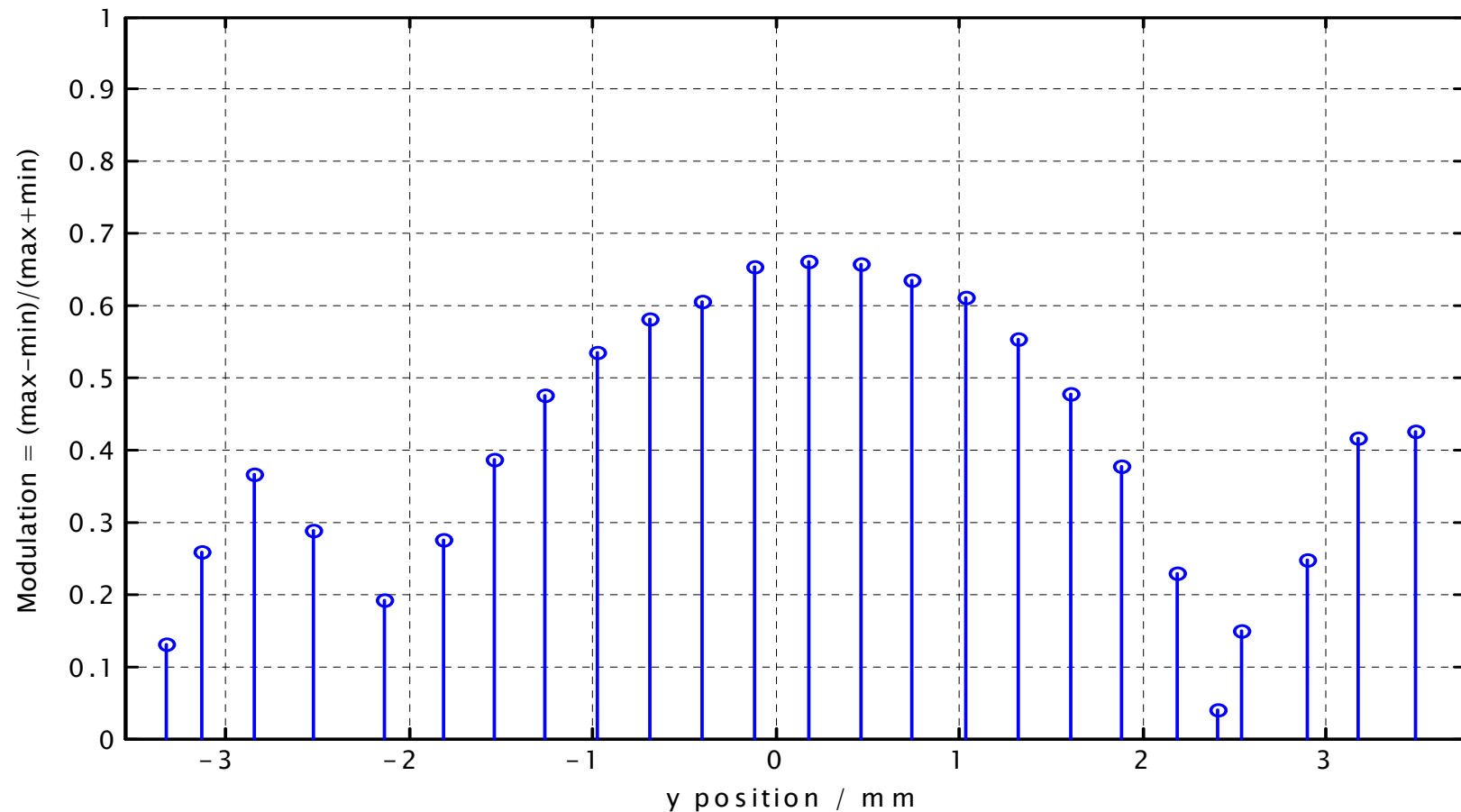
## Smoothed Projection



# Analysis of Experimental Data

## Modulation Depth

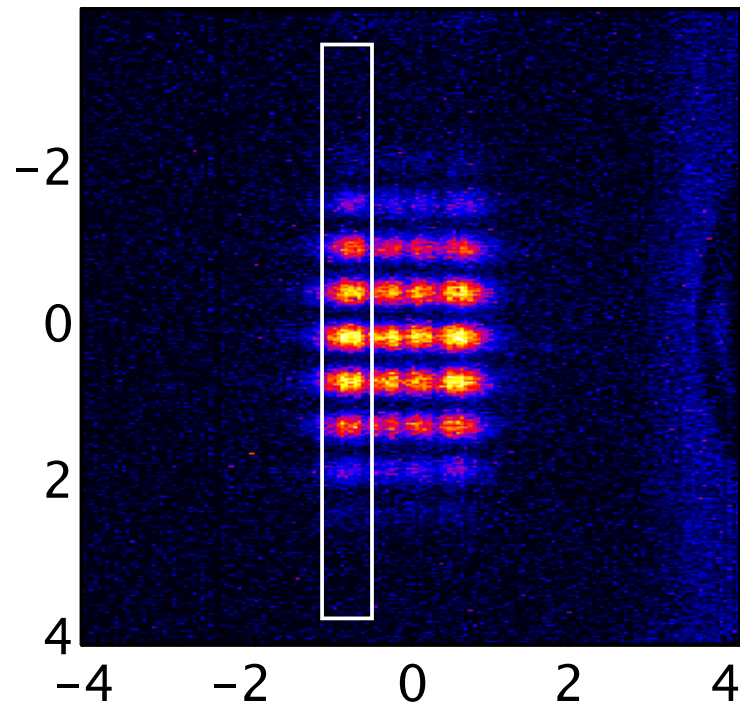
$$\text{modulation} = \frac{\text{max} - \text{min}}{\text{max} + \text{min}}$$



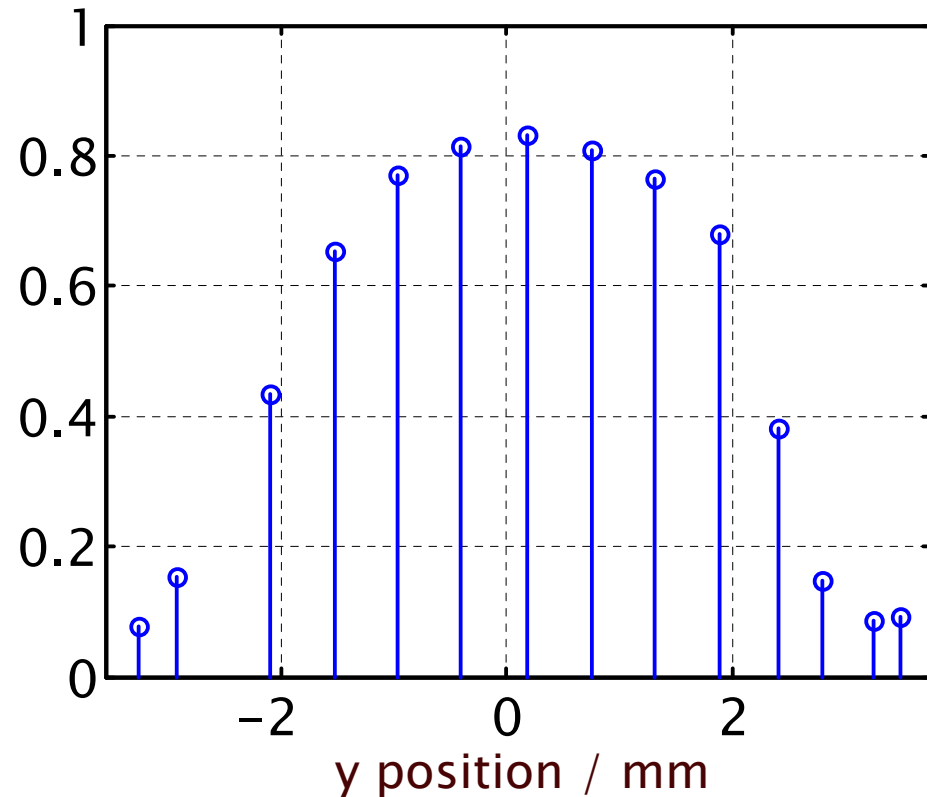
## Analysis of Experimental Data

# Double Slit — 0.5 mm separation

Reconstructed Image



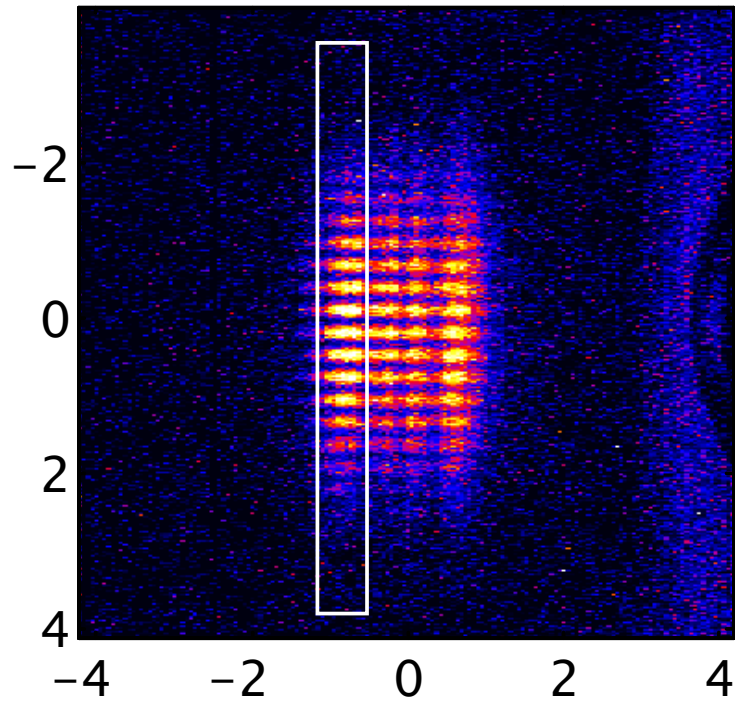
Modulation



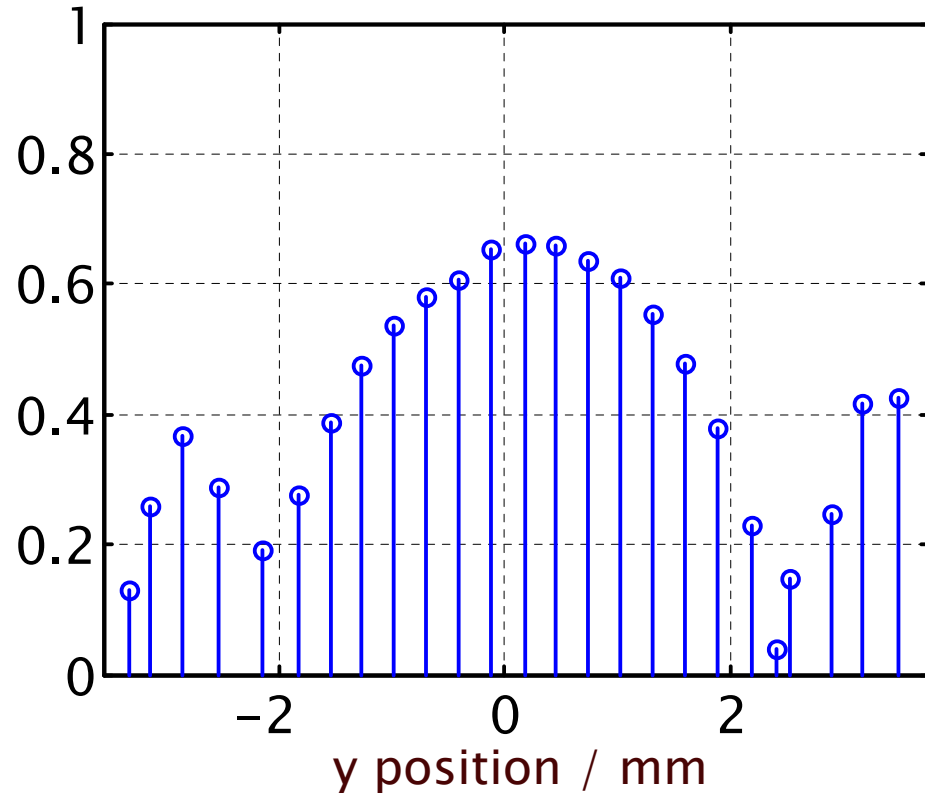
Analysis of Experimental Data

# Double Slit — 1 mm separation

Reconstructed Image



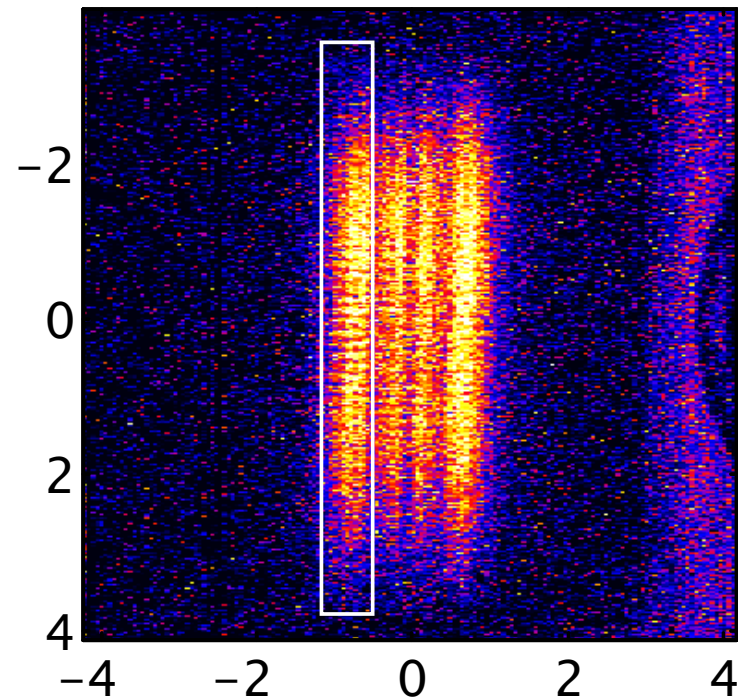
Modulation



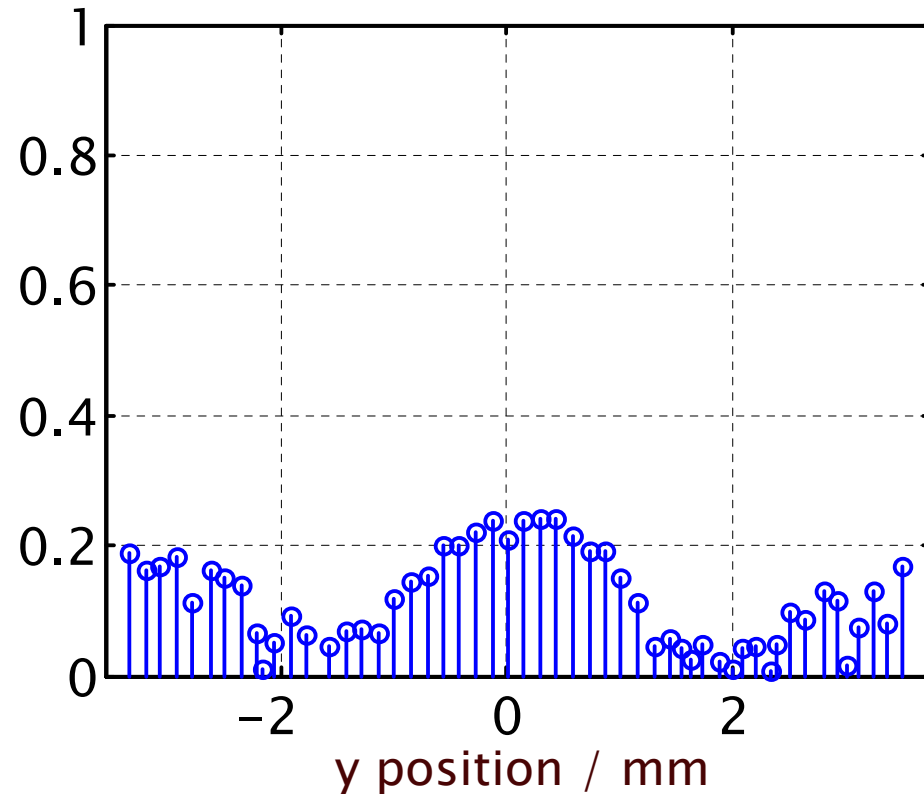
## Analysis of Experimental Data

# Double Slit — 2 mm separation

Reconstructed Image



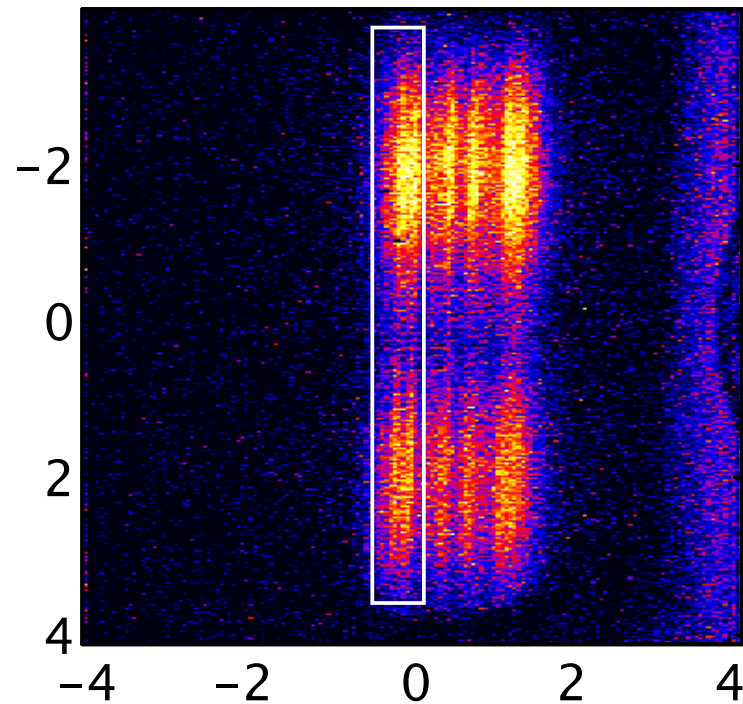
Modulation



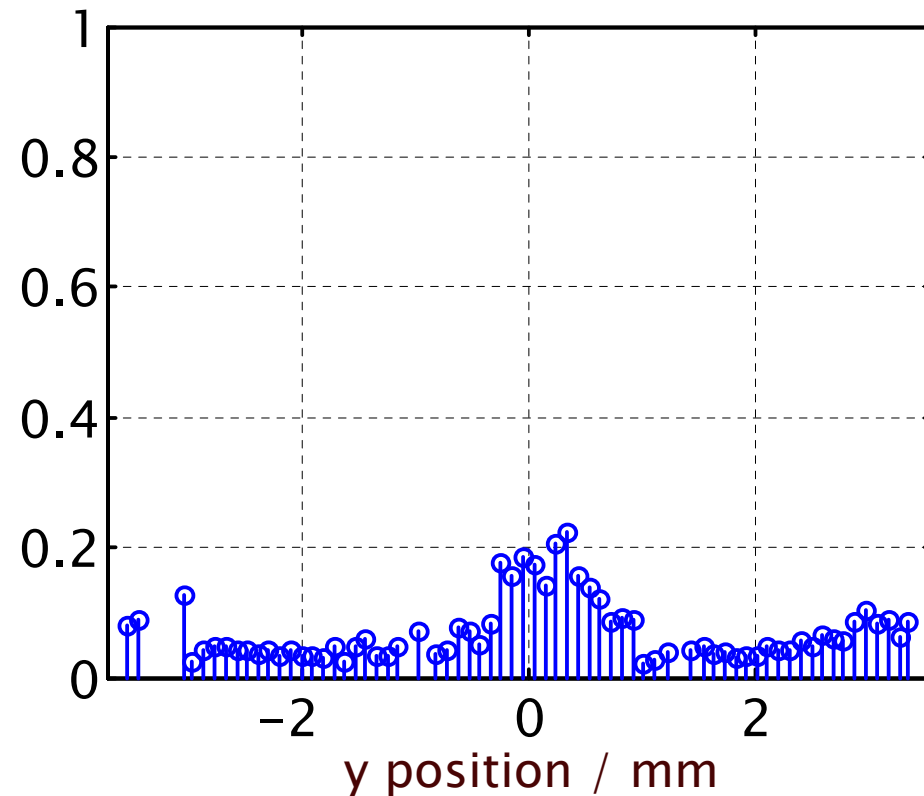
Analysis of Experimental Data

# Double Slit — 3 mm separation

Reconstructed Image

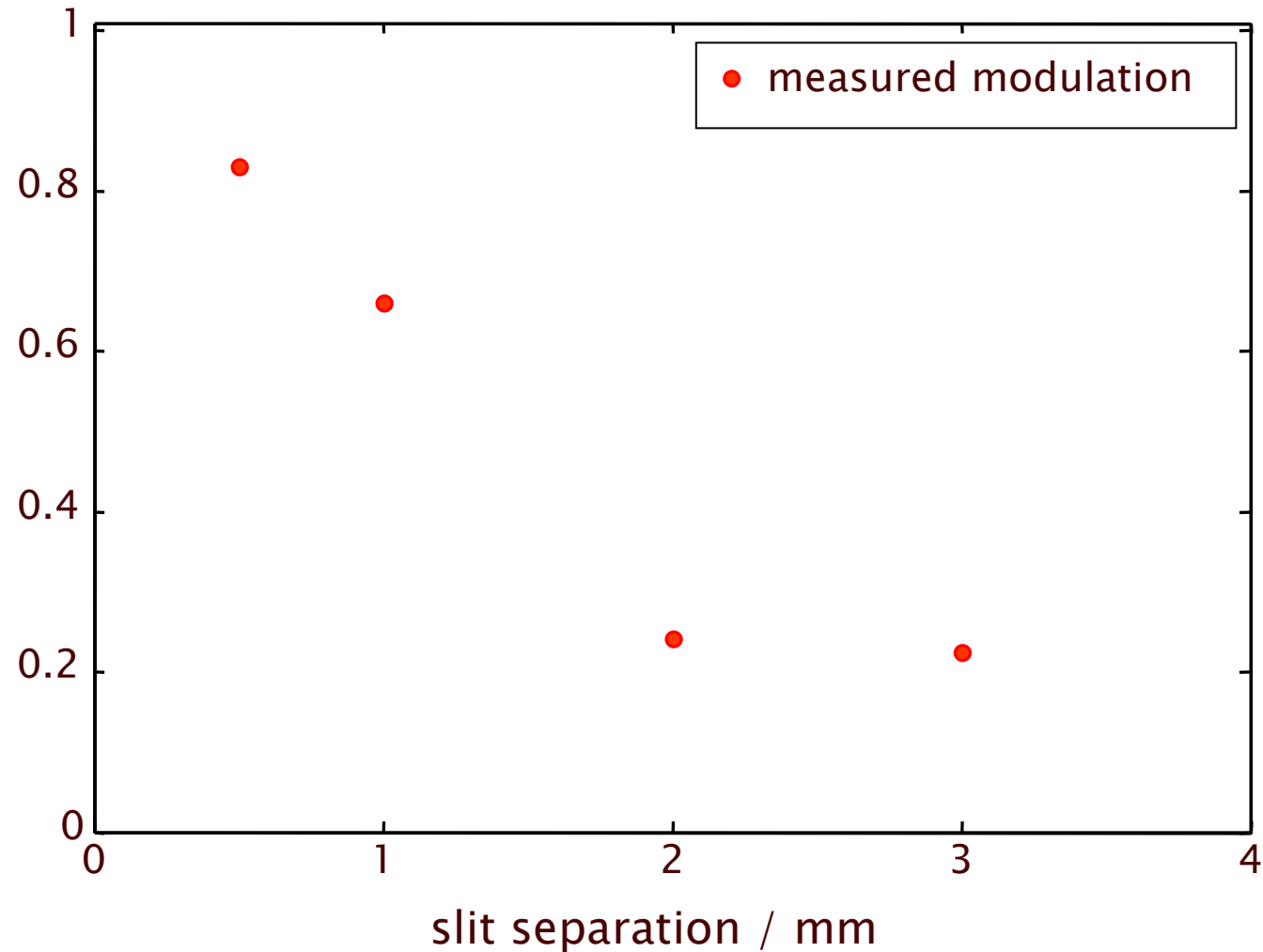


Modulation



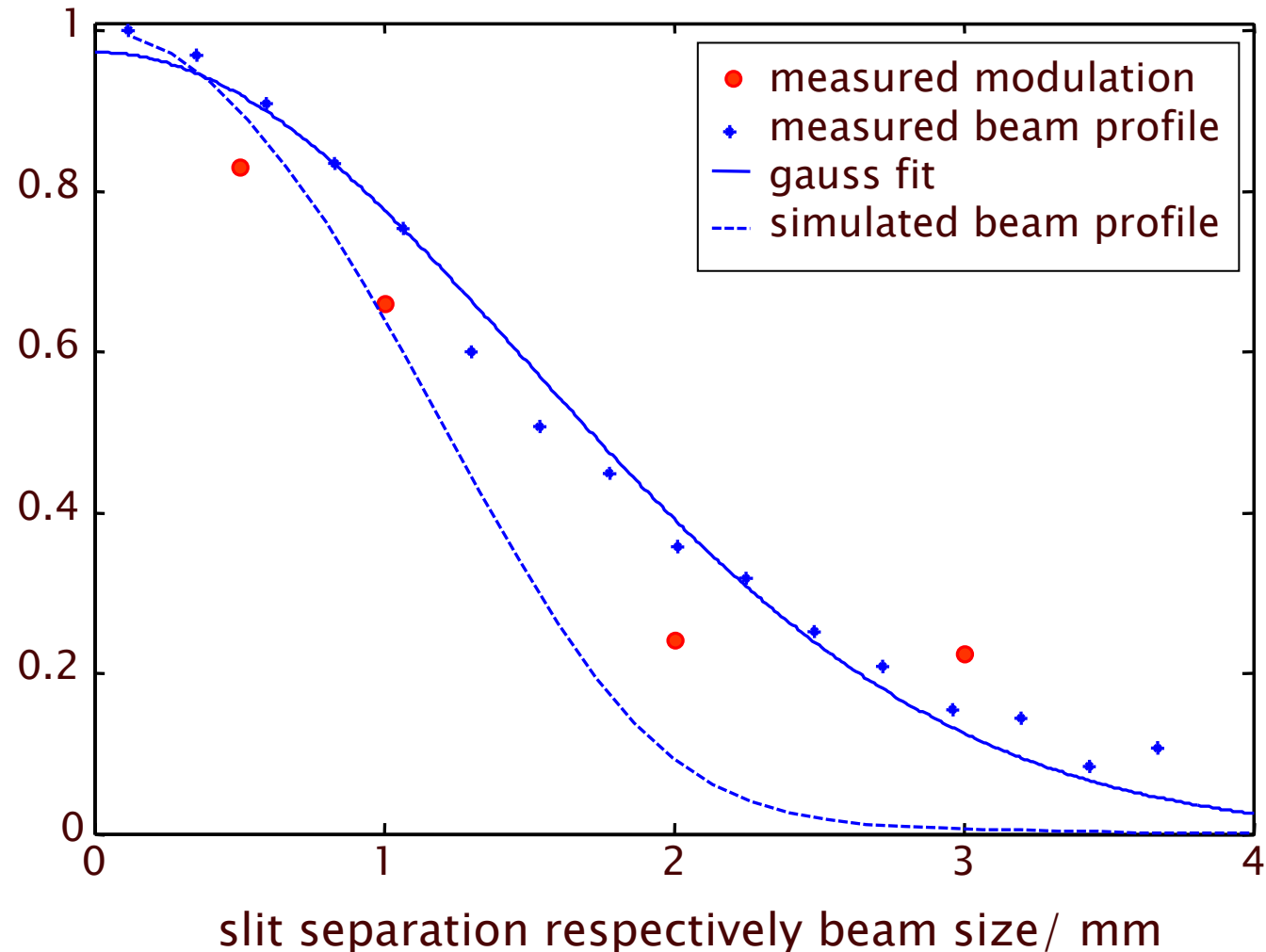
Analysis of Experimental Data

# Slit Separation $\rightarrow$ Modulation



Analysis of Experimental Data

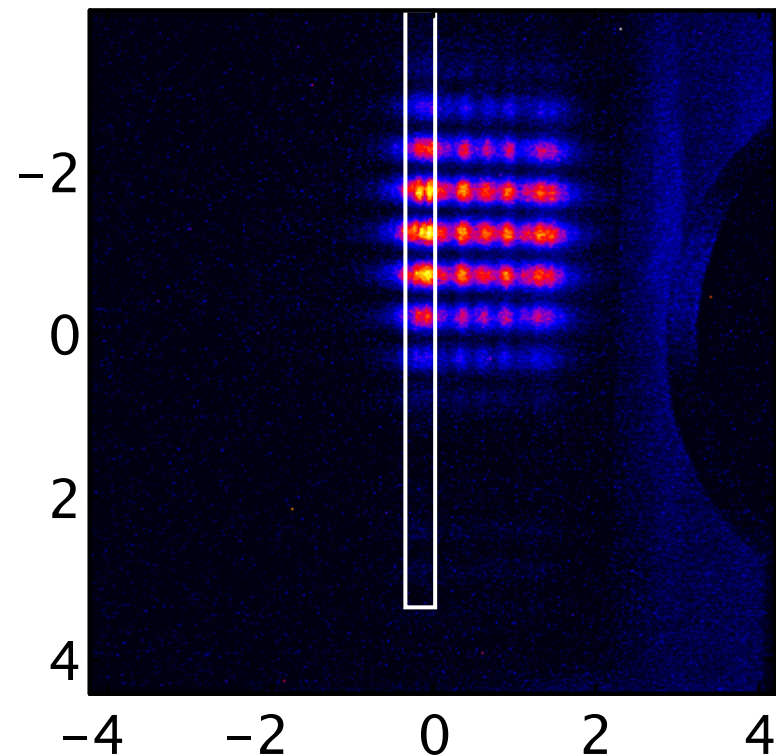
# Slit Separation $\rightarrow$ Modulation



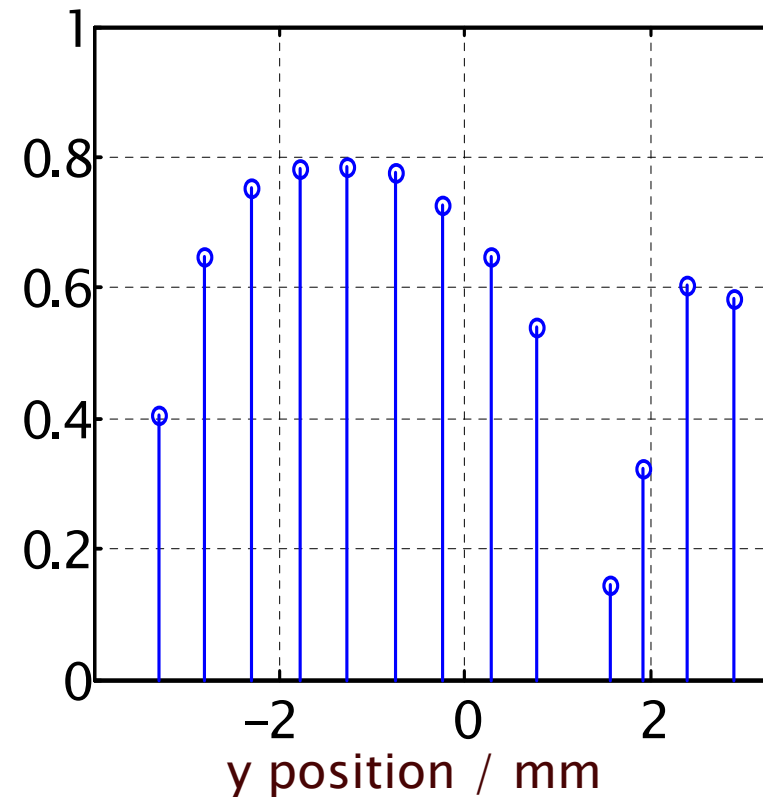
Analysis of Experimental Data at 87 nm

# Double Slit — 0.5 mm Separation

Reconstructed Image



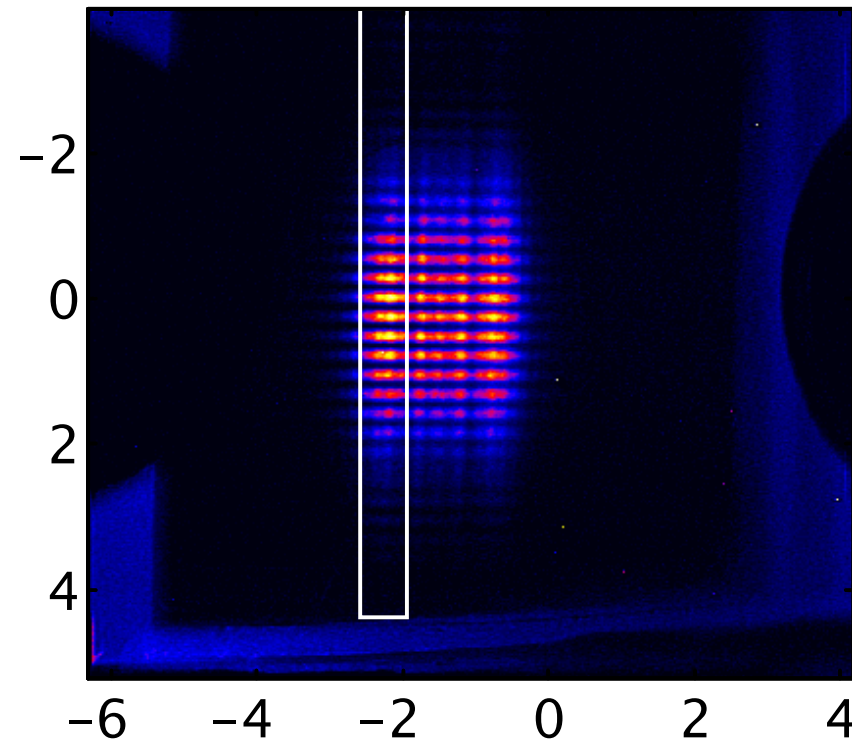
Modulation



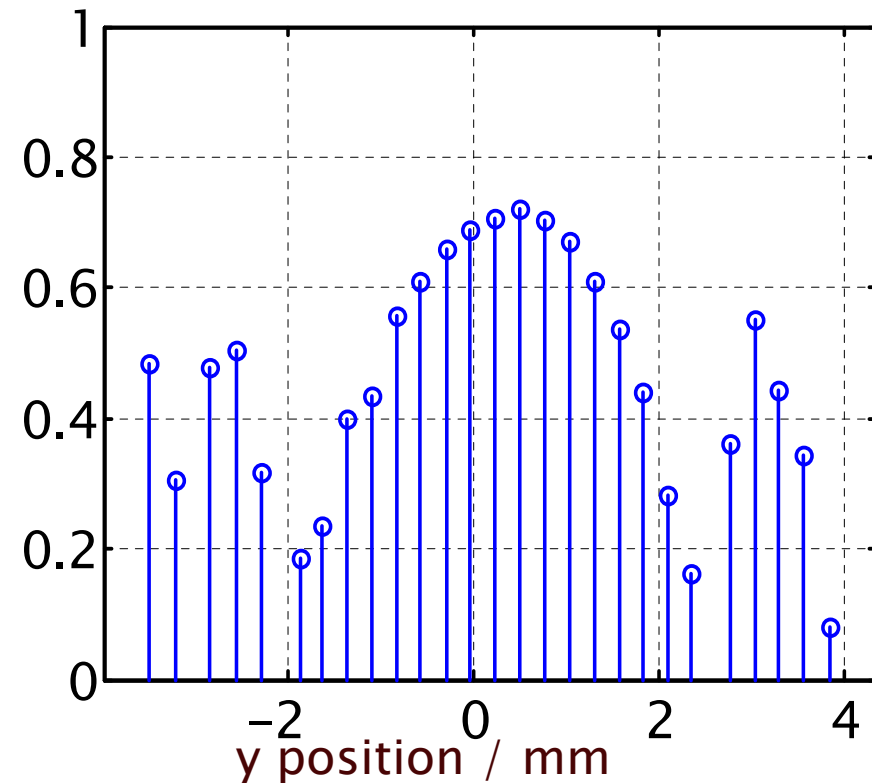
Analysis of Experimental Data at 87 nm

# Double Slit — 1 mm Separation

Reconstructed Image

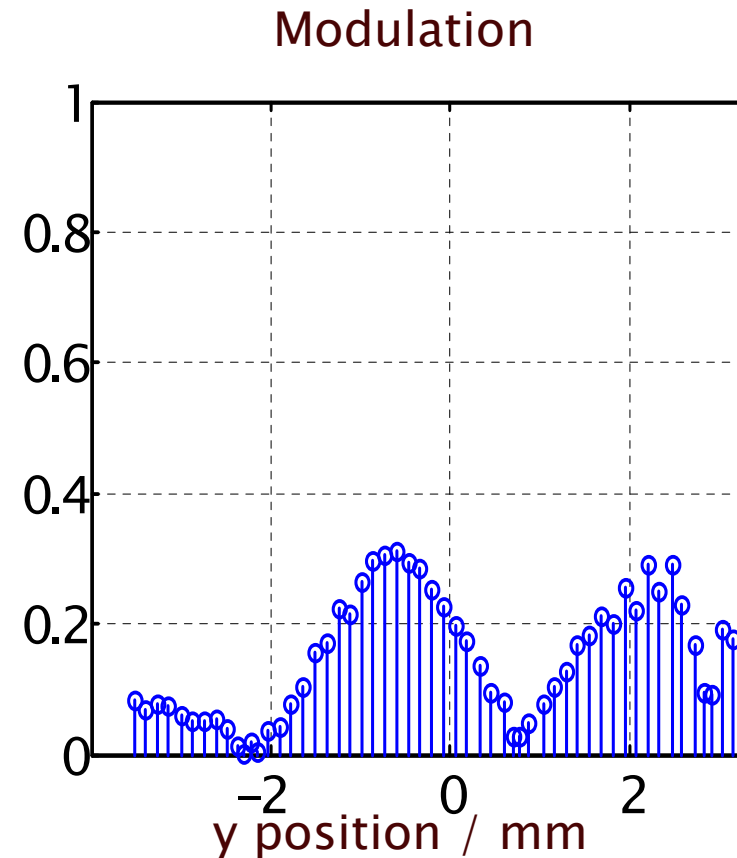
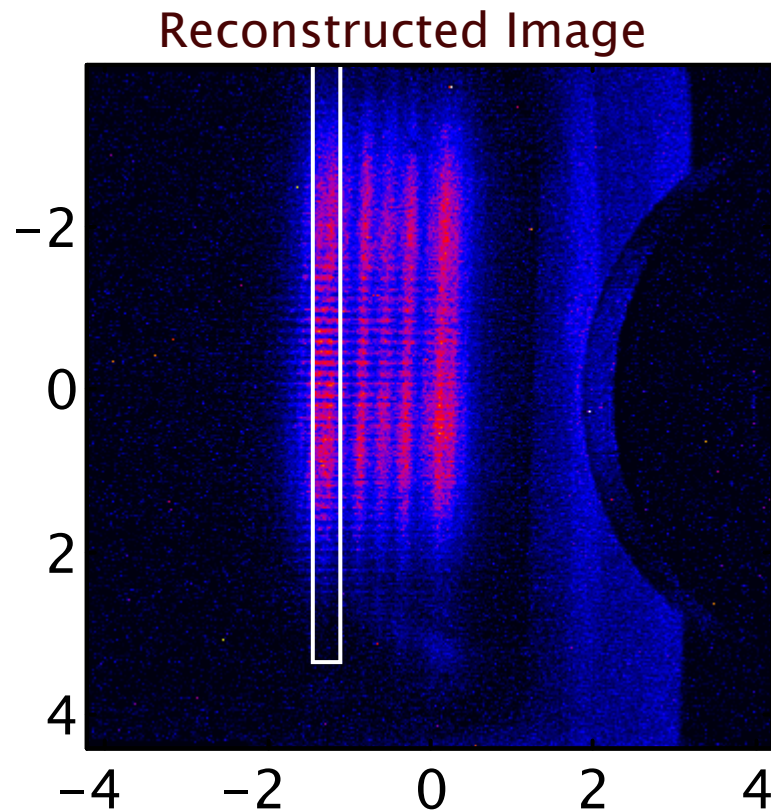


Modulation



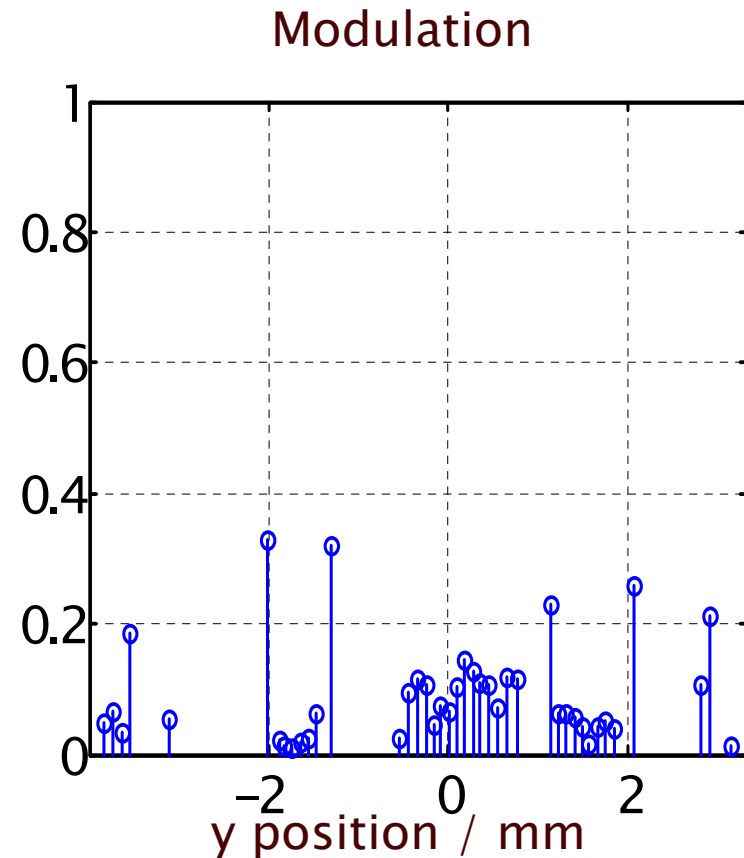
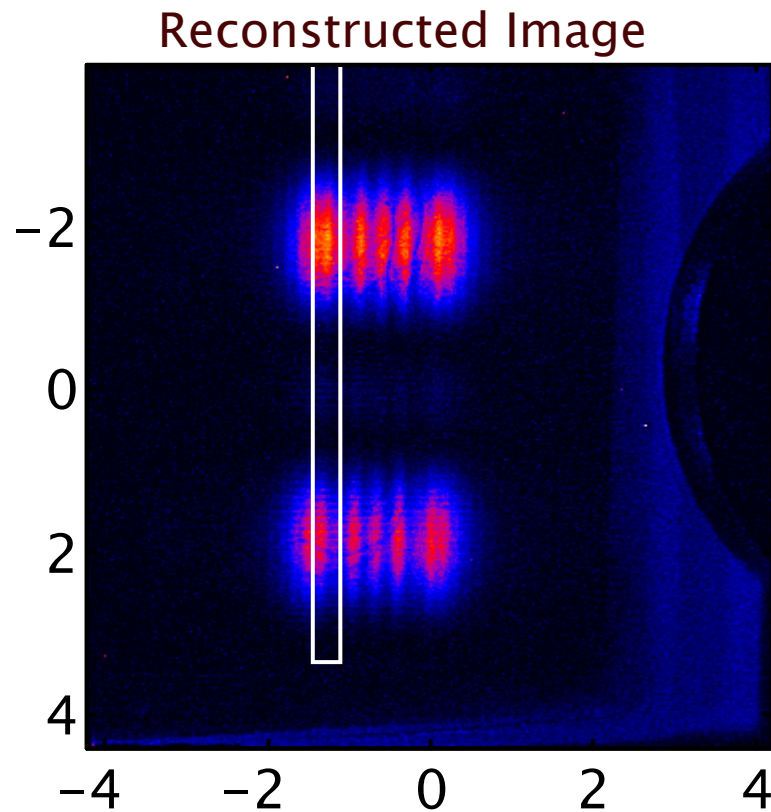
Analysis of Experimental Data at 87 nm

# Double Slit — 2 mm Separation



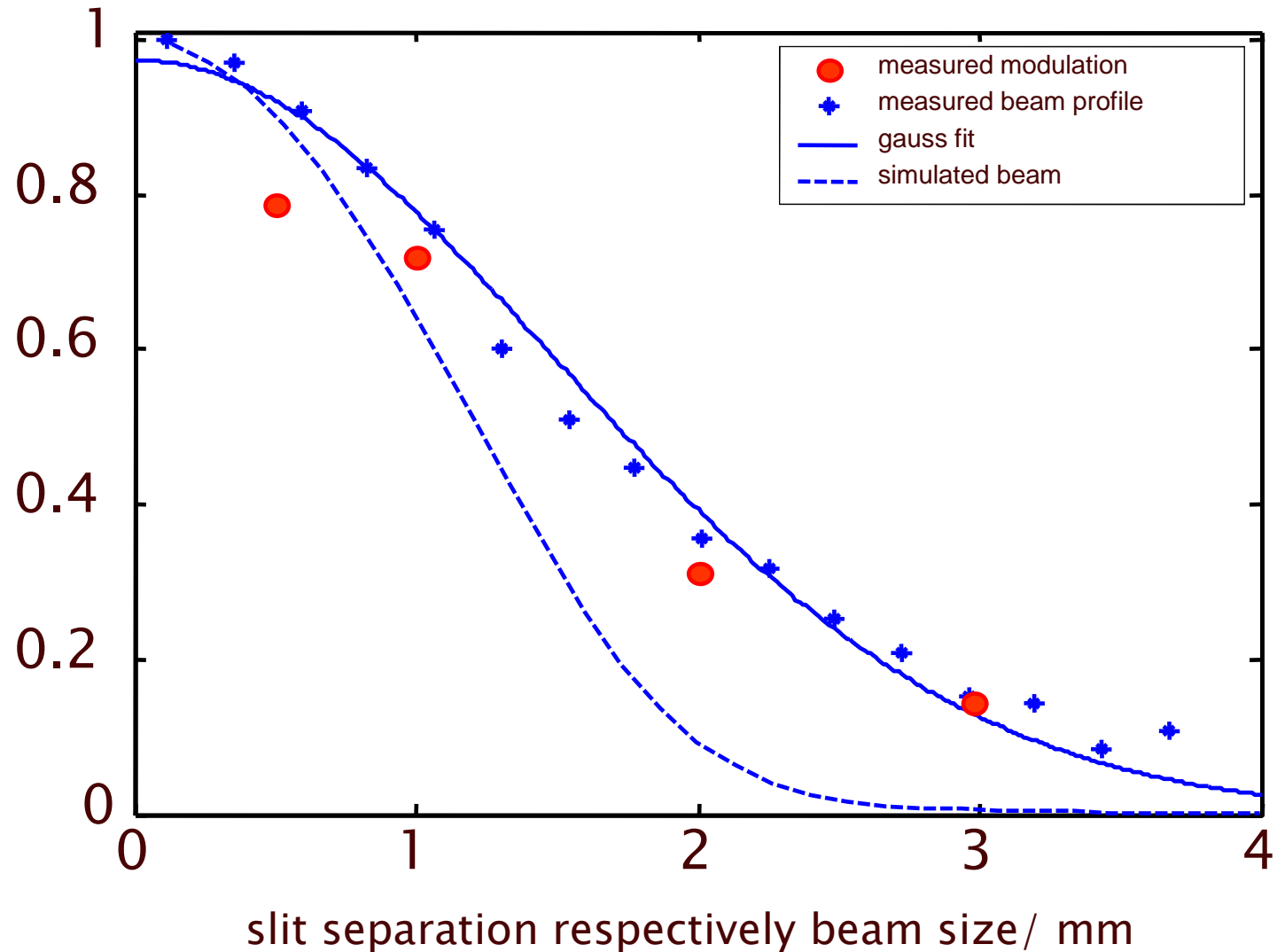
Analysis of Experimental Data at 87 nm

# Double Slit — 3 mm Separation



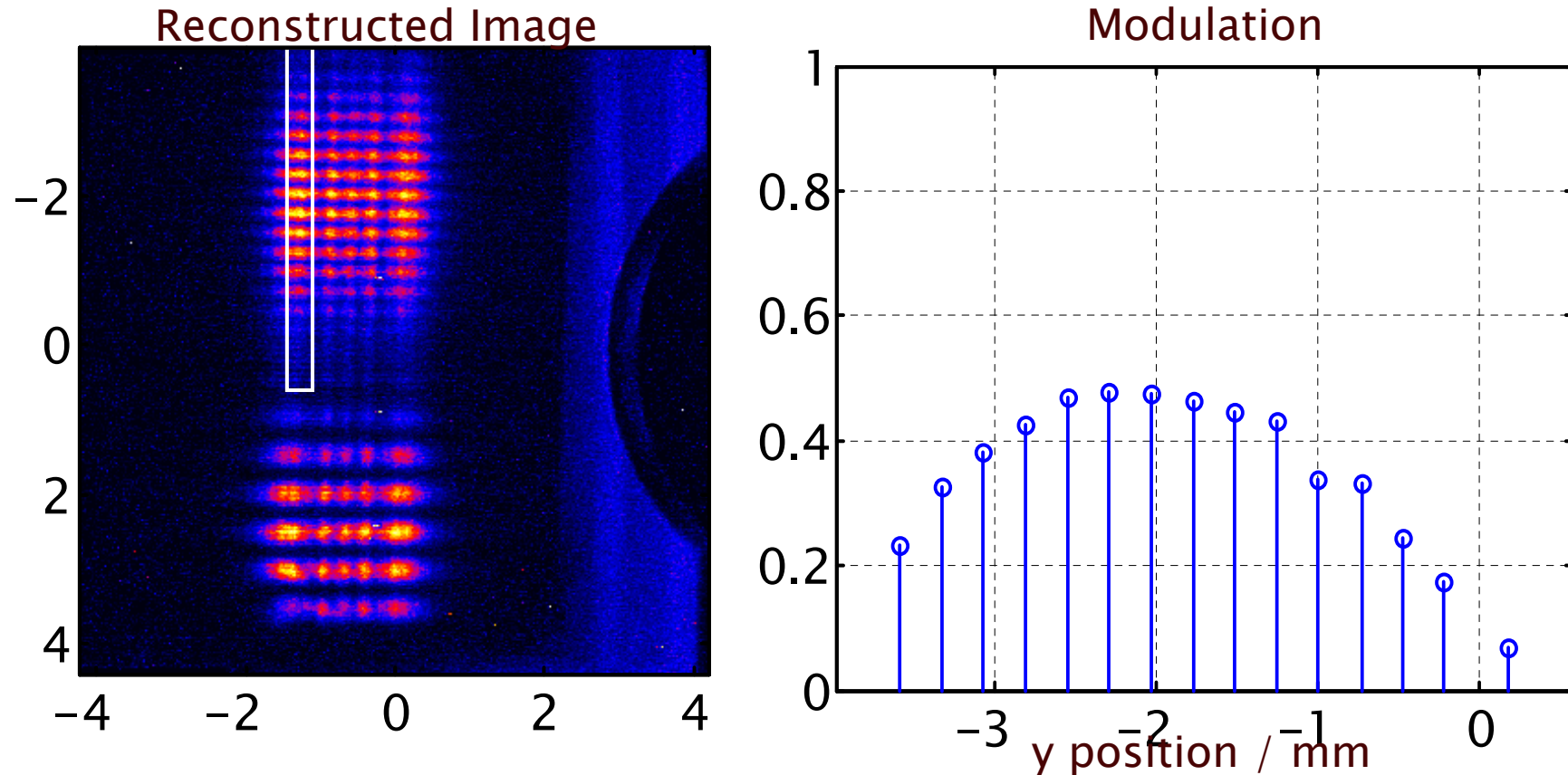
Analysis of Experimental Data at 87 nm

# Dependence on Slit Separation



## Analysis of Experimental Data

# Coherence in the Outer Part of the Beam



# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

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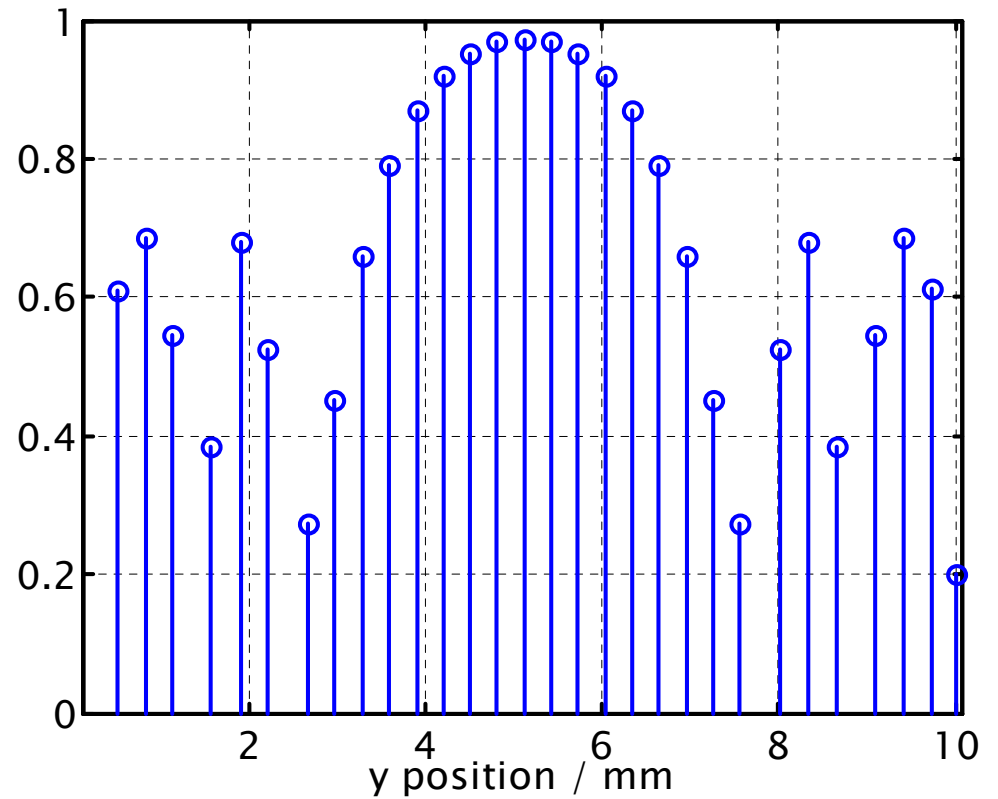
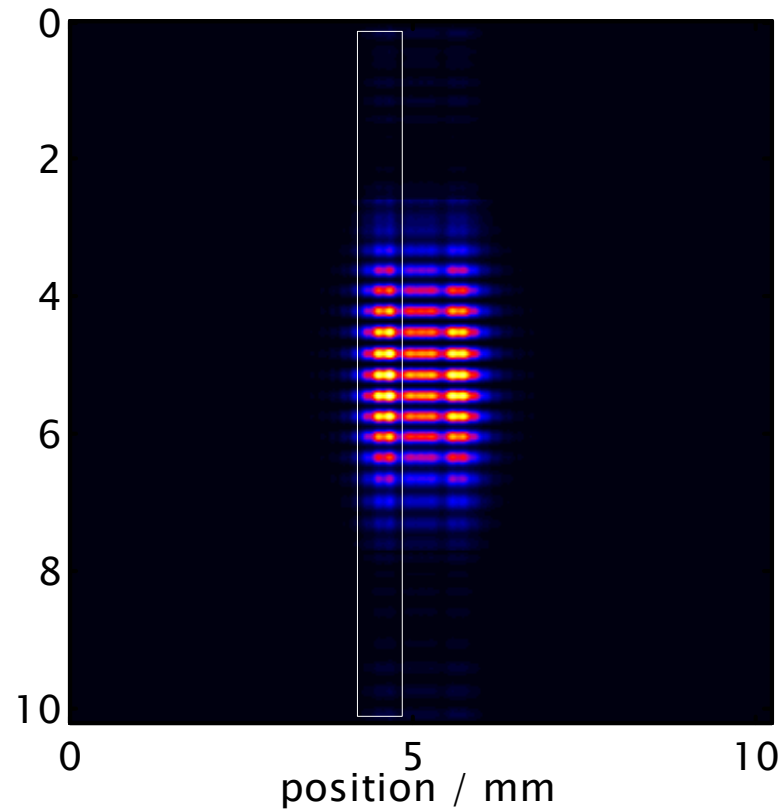
## Simulations

# GLAD

- “General Laser Analysis and Design”
- Calculates the diffraction in the near field
- Propagates arbitrarily shaped wave packets, defined by slowly varying amplitude
- Various optical elements
- Import and export of the electric field
  
- Limitations
  - Assigned memory not sufficient to propagate 3-dimensional beam (defined on 1024x1024x512 points)

Simulations

# Plane Wave Input

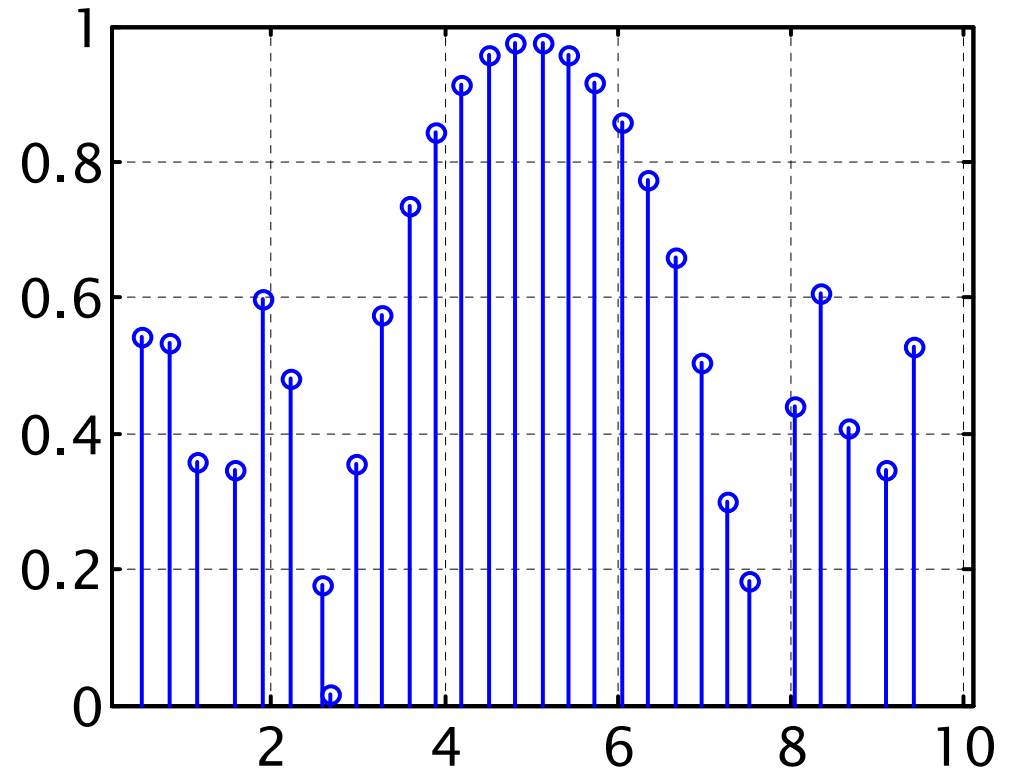
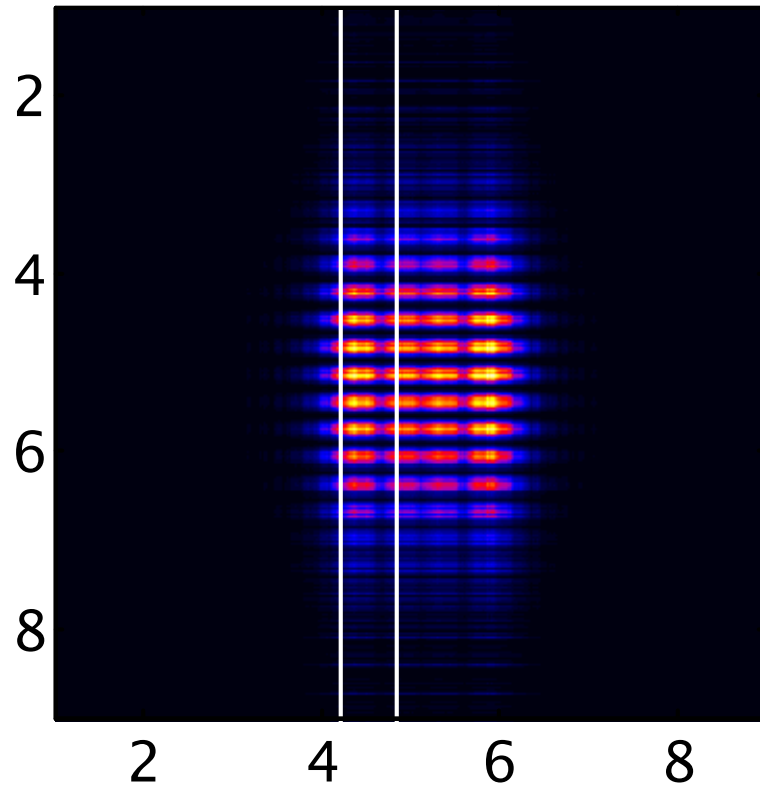


## Simulations

# FAST

- Saldin, Schneidmiller, Yurkov
  - 3-dimensional Free Electron Laser code
    - Start from shot noise
    - Numerical solution of the initial-value problem
    - Non-Linear Dynamics of the FEL process
      - ⇒ Predicts
        - Transverse mode selection
        - Saturation
  - Delivers the electric field (in Slowly Varying Amplitude approximation) at the exit of the undulator
- ↪ Input file for GLAD

# Simulations FAST



# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

- Introduction
  - TTF Linear Accelerator and Free Electron Laser
  - Photon Diagnostics
  - Near Field Diffraction Effects
- Measurements
- Image Processing
- Analysis
- Simulations
- **Consistency of the Measurements**
- Development of Transverse Coherence
- Outlook

# Comparison with other Methods

- Coherence of the FEL is given by the number of independent modes
- Here: transverse coherence  $\leftrightarrow$  number of transverse modes
- For the fundamental gaussian mode, we have at the waist:

$$\sigma_r \sigma_\theta = \lambda / 4\pi$$

where  $\sigma_r$  is the beam diameter,  $\sigma_\theta$  the angular divergence

- For higher order modes:

$$\sigma_r \sigma_\theta \geq \lambda / 4\pi$$

## Consistency of the Measurements

# Comparison with other Methods

- Consider a perfectly coherent beam, where only the fundamental gaussian mode is present:

$$\sigma_r \sigma_\theta = \lambda / 4\pi$$

easy to measure

easy to measure (distribution in the far field)

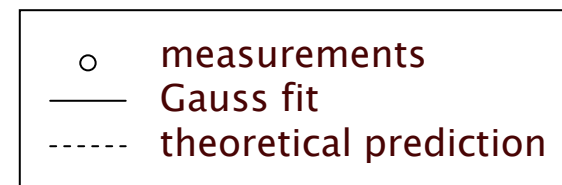
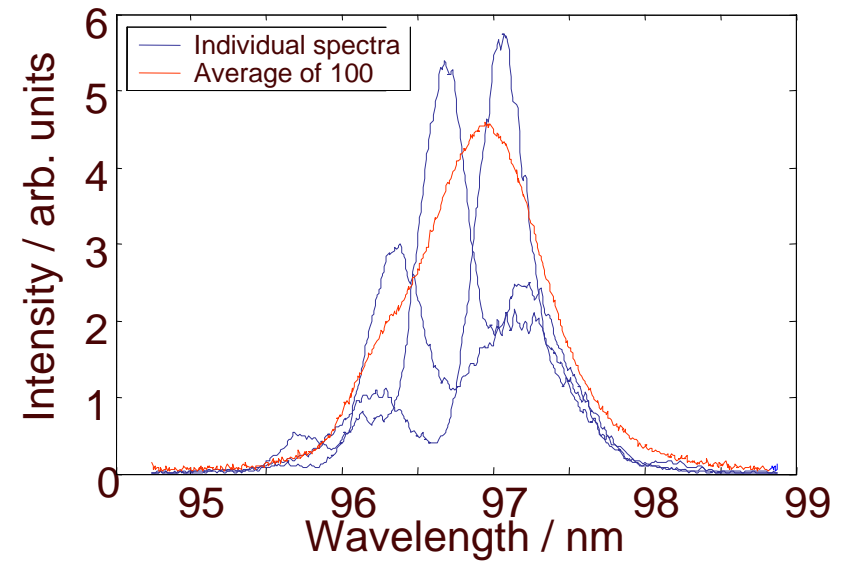
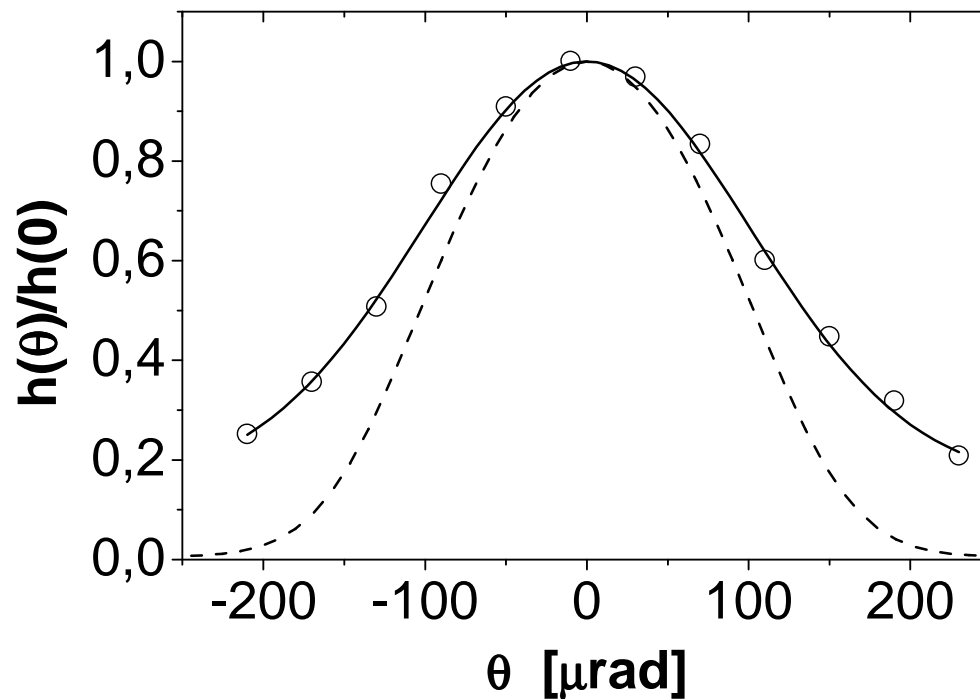
determine photon beam size in the undulator

## Consistency of the Measurements

# Comparison with other Methods

Measurement:  $\lambda = 97 \text{ nm}$

$\sigma_\theta = 120 \text{ } \mu\text{rad}$ :



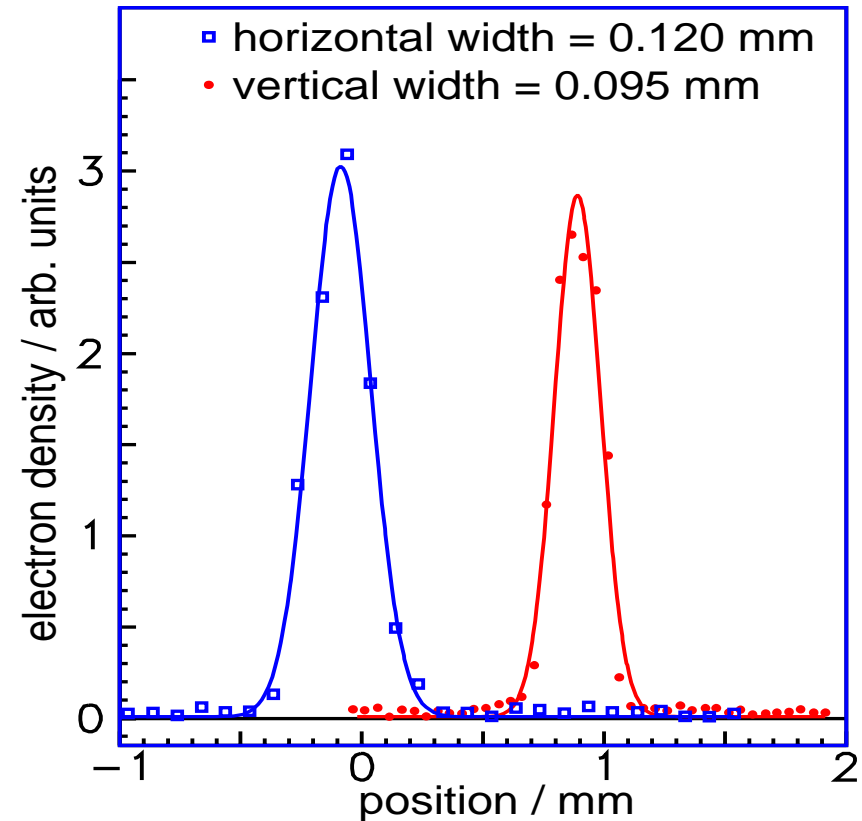
## Consistency of the Measurements

# Comparison with other Methods

⇒ For the fundamental transverse mode, we expect a photon beam width

$$\sigma_r = 64 \mu\text{m}$$

- Compare to the electron beam in the undulator:



# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

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Outlook

# Development along Undulator

- Beyond the saturation of the FEL:  
growth of the number of transverse modes
- ⇒ decrease of transverse coherence!
- TTF FEL can be virtually shortened by kicking the beam off the undulator axis
    - measure coherence at different effective undulator lengths

# A Double Slit Experiment to Study the Transverse Coherence of the TTF FEL

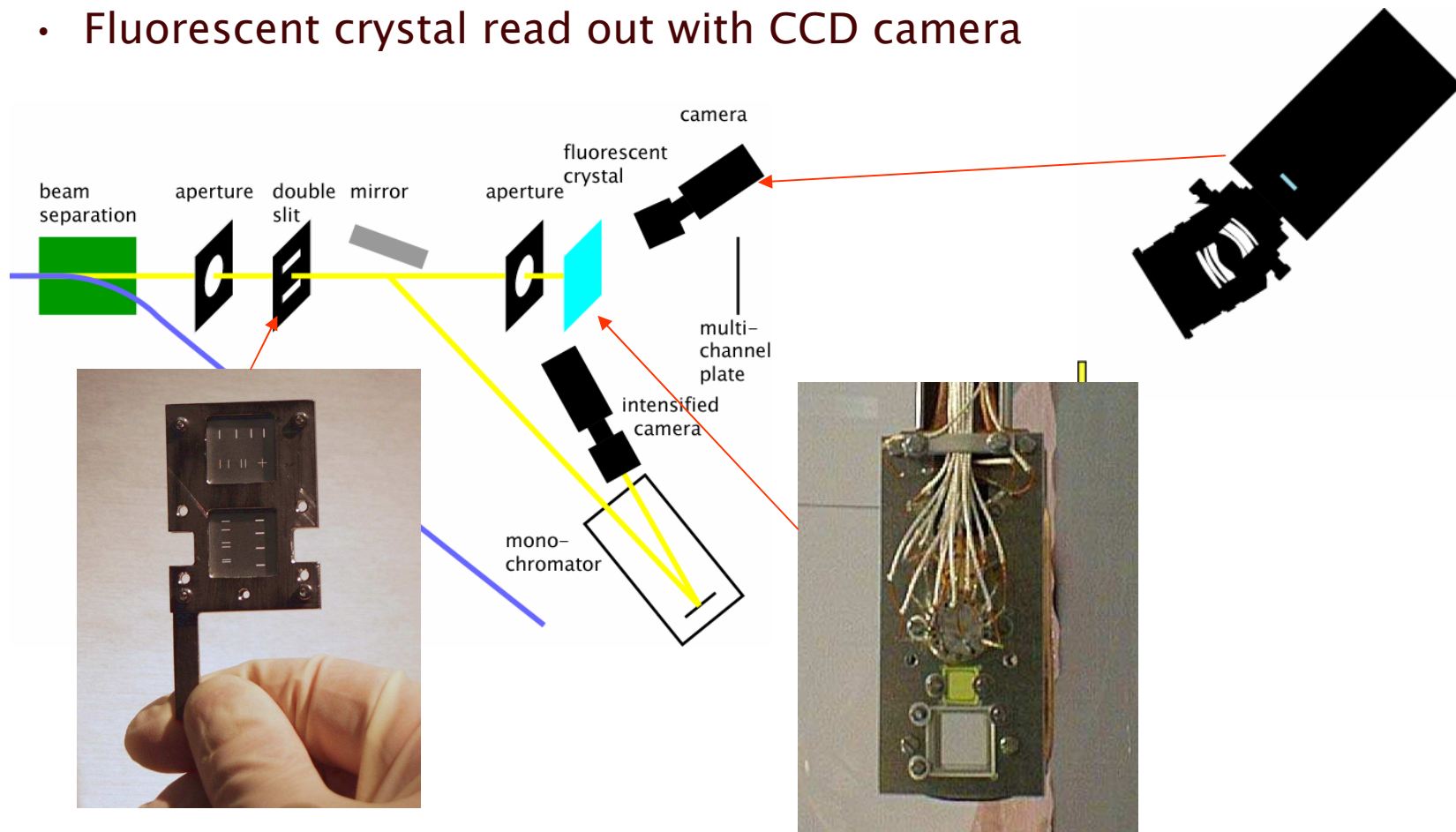
- Introduction
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# Outlook

- Refinement of the Analysis
  - Consider influence of multiple scattering in the fluorescent crystal
  - What is the effect of the averaging over many pulses?
- Expansion of the Analysis
  - Degree of coherence at various Undulator lengths
- Can this device be installed at X-Ray wavelengths?

# Coherence Measurements Conclusion (1)

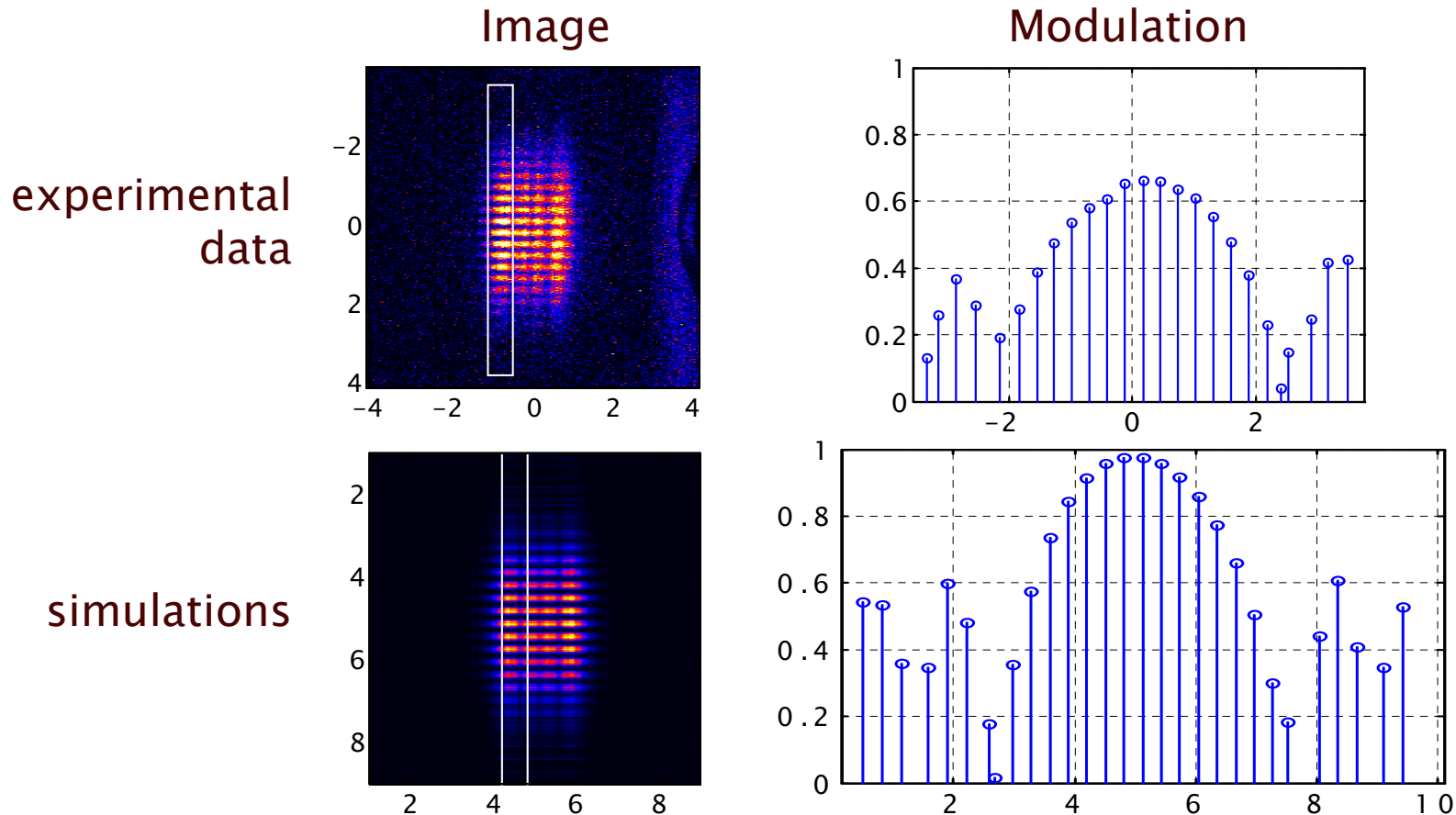
- Obtained double slit diffraction patterns of a SASE FEL at 100 nm
  - Set-Up in ultra high vacuum
  - Fluorescent crystal read out with CCD camera



# Coherence Measurements

## Conclusion (2)

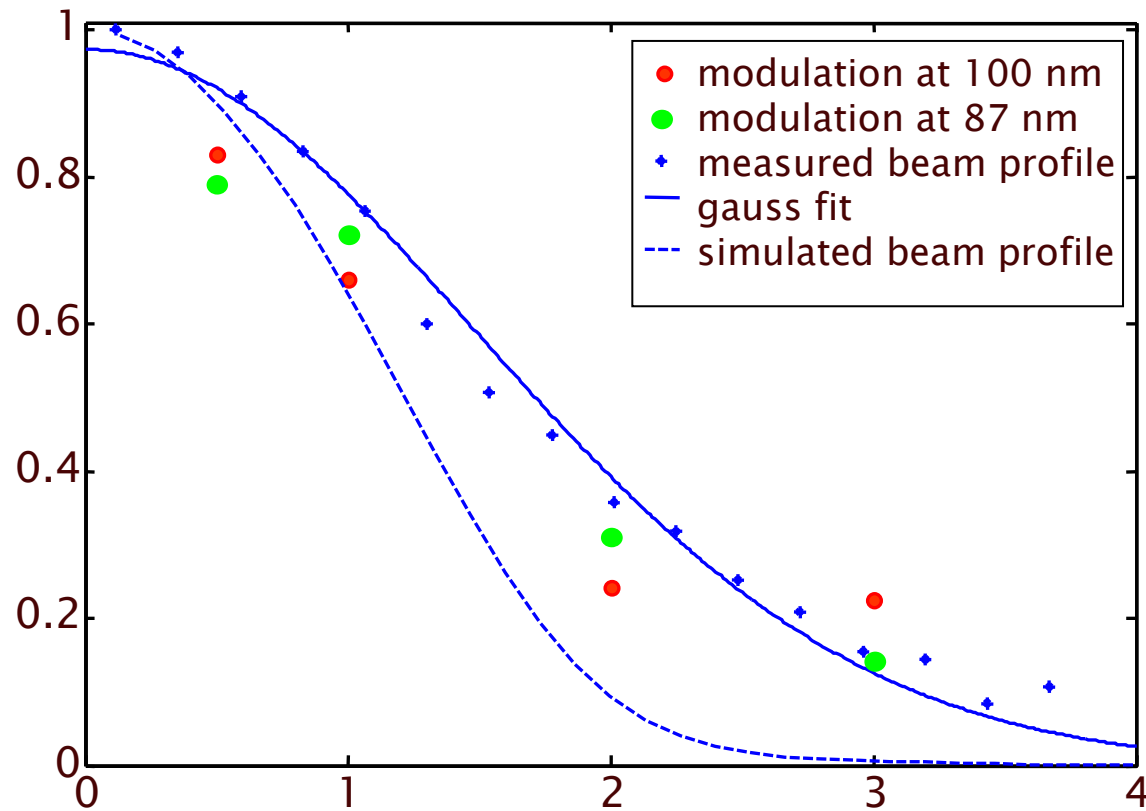
- Double slit create diffraction images similar to near field theory:
  - Modulation depth decreases outwards



# Coherence Measurements

## Conclusion (3)

- Determined Modulation
  - at various slit separations
  - with different electron bunch properties



# Contributions by

- J. Feldhaus, Ch. Gerth, P. Kulinski, E. Saldin, P. Schmüser, E. Schneidmiller, B. Steeg, K. Tiedtke, M. Tonutti, R. Treusch, M. Yurkov

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